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Franz Käppeler, FZ Karlsruhe  
Karl-Ludwig Kratz, MPI f. Chemie, Mainz*

The Karlsruhe Chart of Nuclides gives the relative proportions for the stable isotopes of chemical elements  
(and the decay modes of unstable nuclei)

**of the Universe**

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The Karlsruhe Chart of Nuclides gives the relative proportions for the stable isotopes of chemical elements (and the decay modes of unstable nuclei)

The chart displays the following information for each nuclide:

- Element Symbol:** Located at the top of each cell.
- Mass Number (A):** Located at the top left of each cell.
- Half-life:** Located in the middle of each cell.
- Decay Mode:** Located at the bottom of each cell.

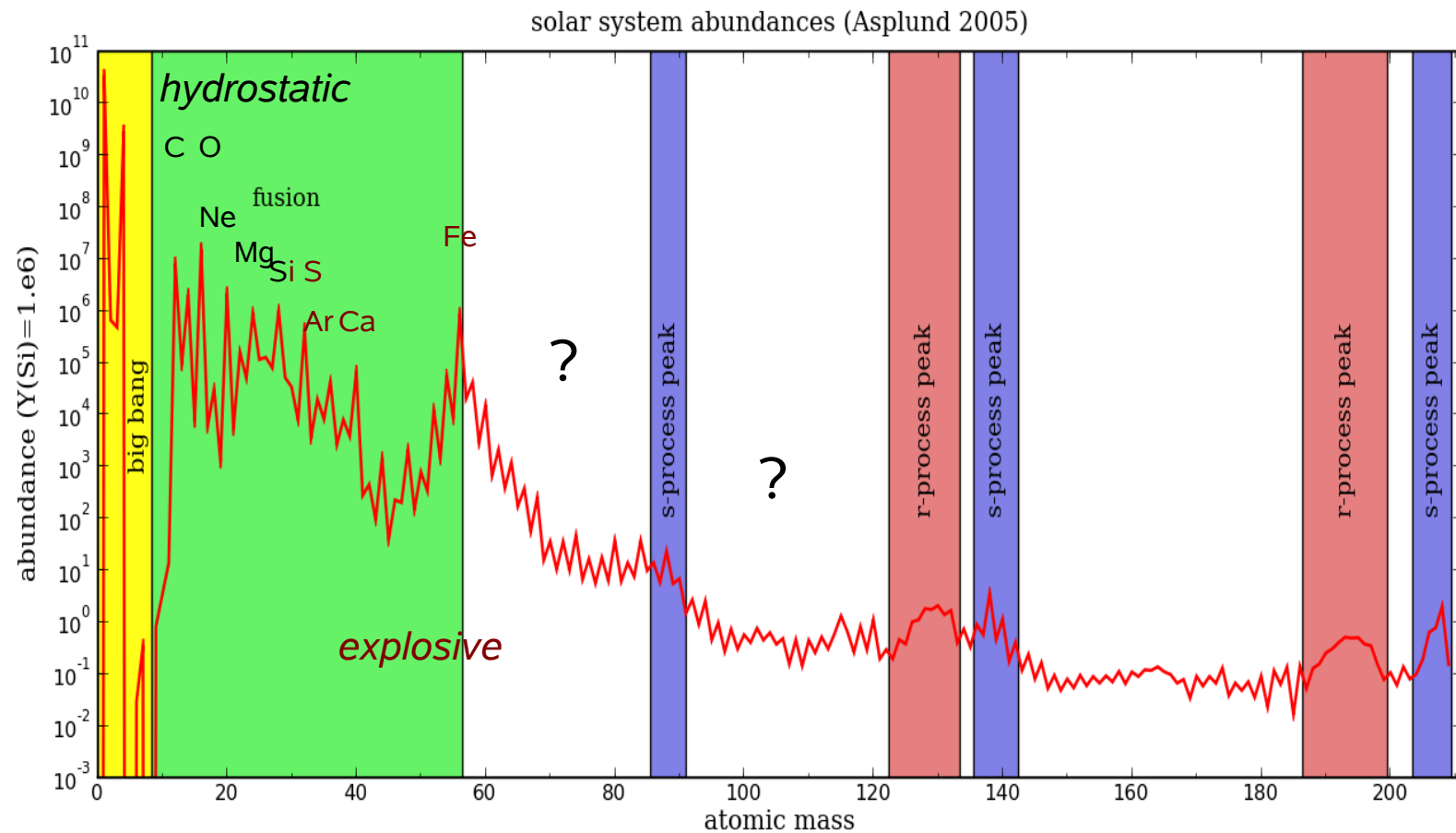
The chart is organized by atomic number (Z) and mass number (A). The elements are listed in columns, and the mass numbers are listed in rows. The chart shows the relative proportions of stable isotopes and the decay modes of unstable nuclei.

# Allende Meteorite

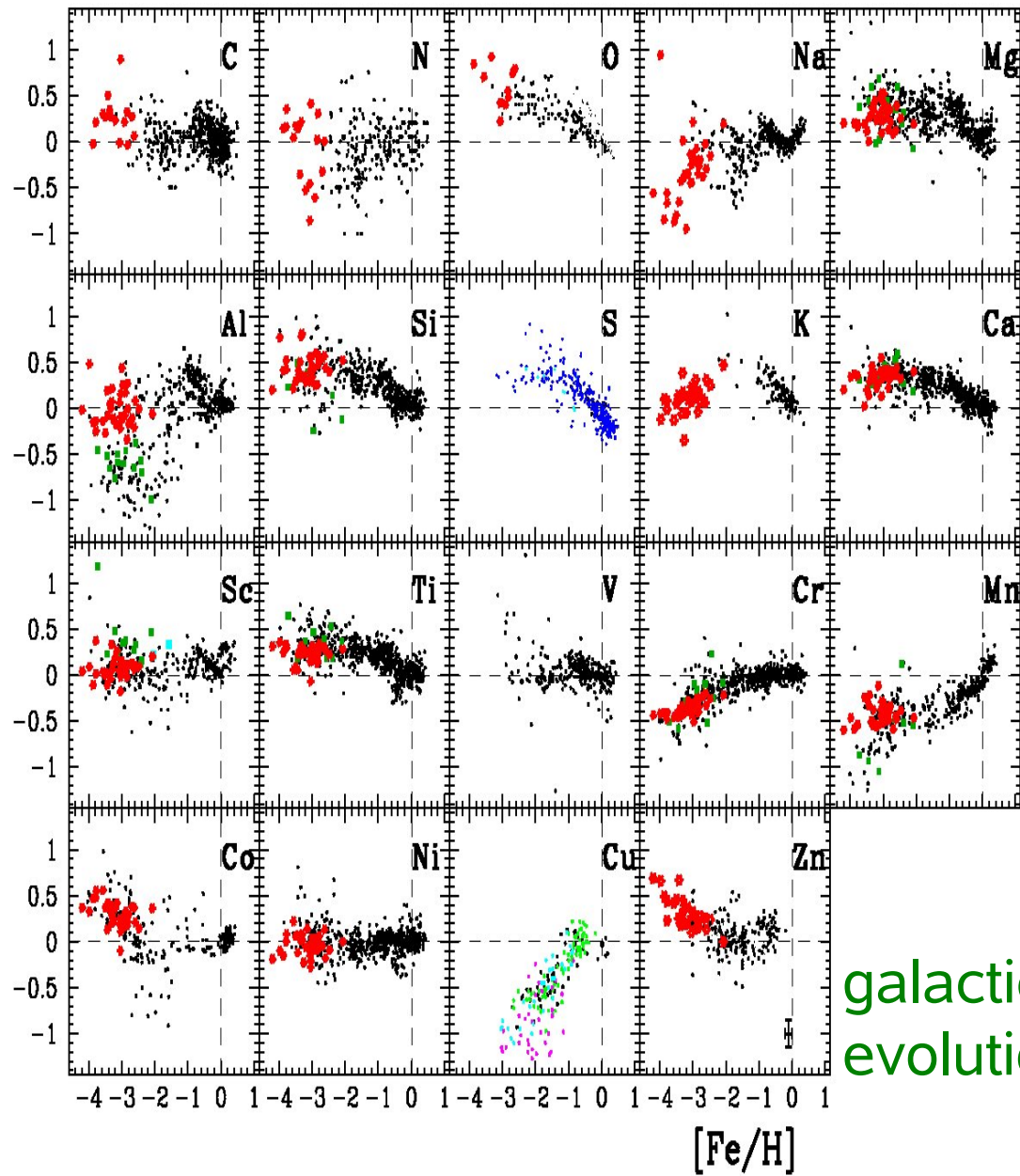
Carbonaceous Chondrites are the most primitive meteorites, matter in their matrix seems not heated beyond 200/50C. They are formed from compacted dust in the outer parts of the solar system. Their elemental ratios reflect the global abundances in the solar system, with the exception of volatile elements (especially noble gases), which might be partially depleted.



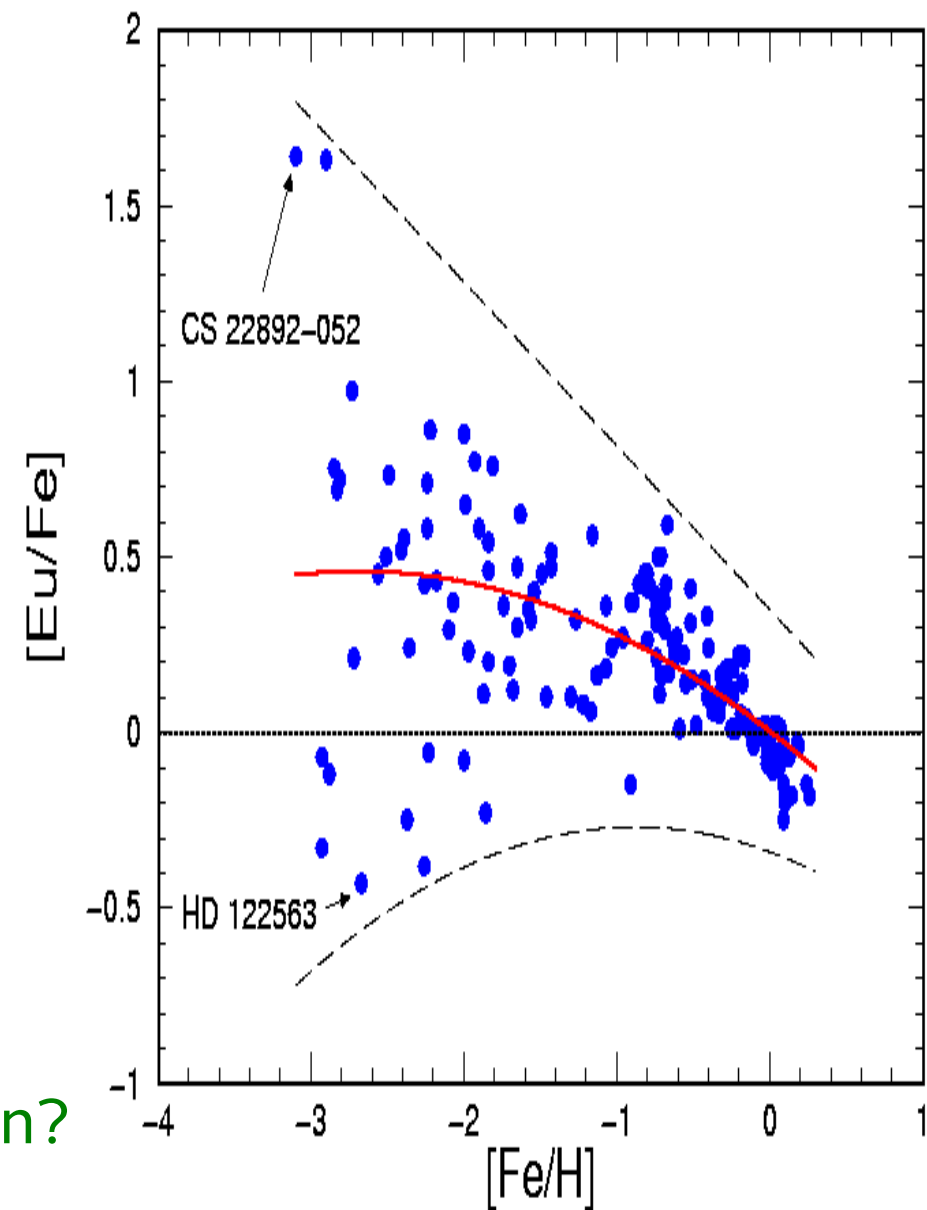
# solar system abundance distribution (from carbonaceous chondrites and solar absorption spectra)



How do we understand solar system abundances.. (plotted are surface abundances of stars)



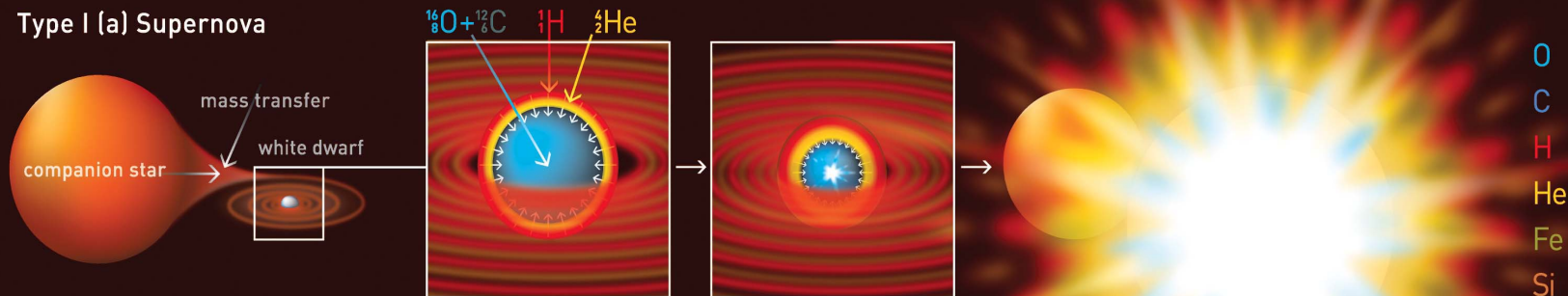
low metallicity stars ...



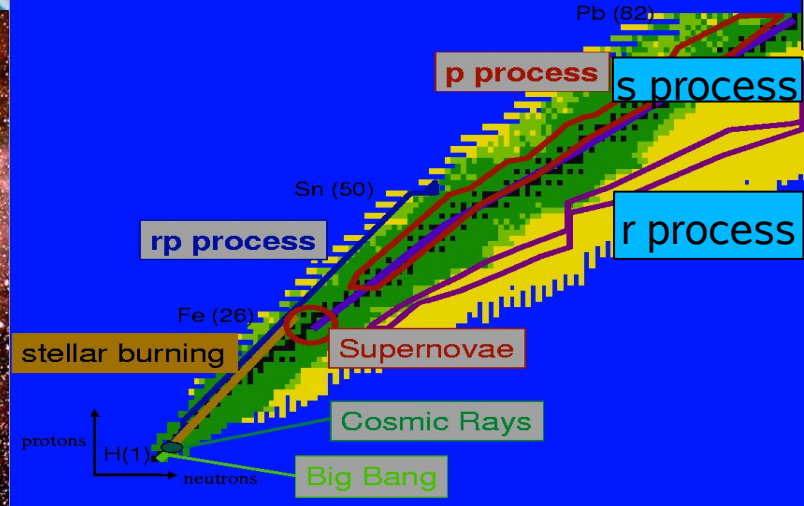
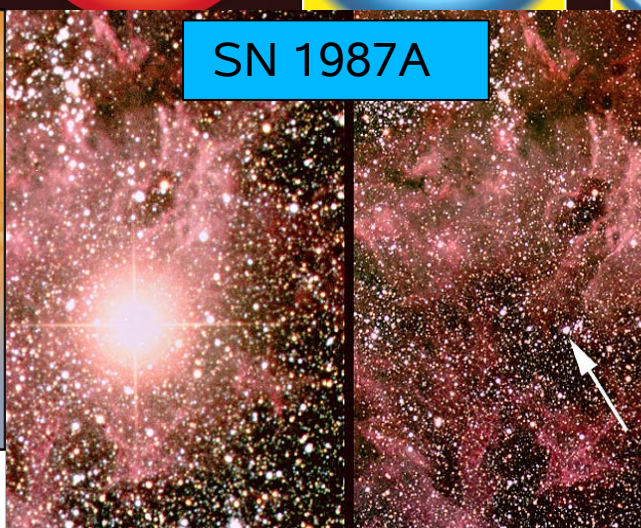
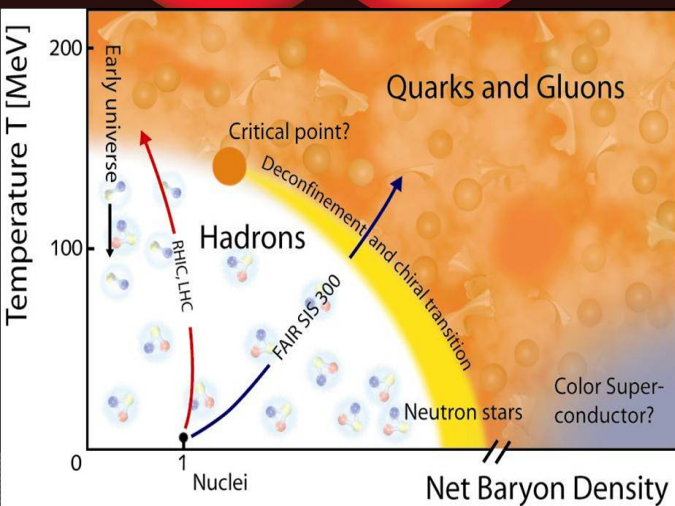
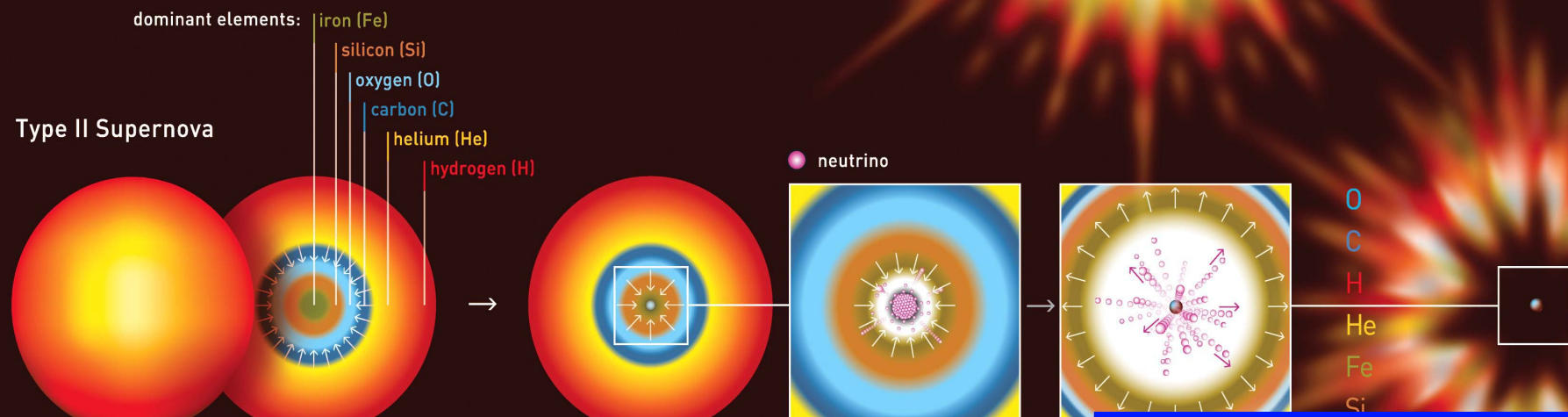


# Supernovae

Type I (a) Supernova



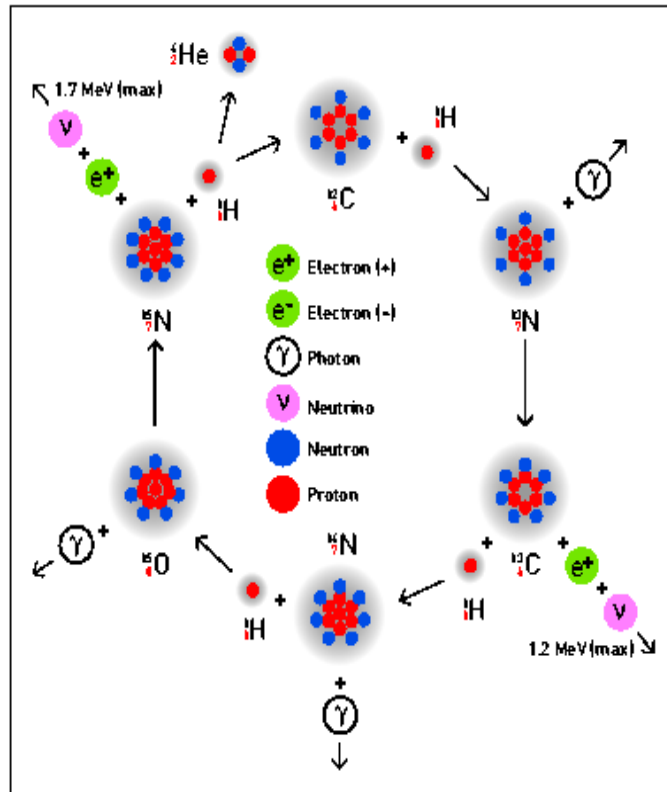
Type II Supernova



# Stellar Burning Stages

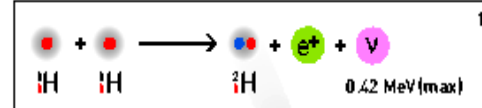
## Hydrogen Burning

### The CNO Cycle

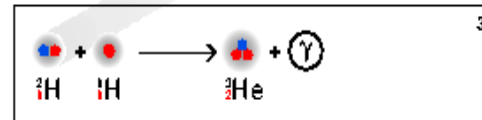
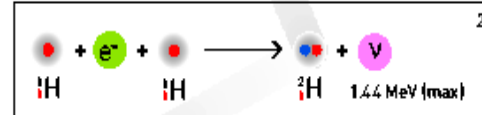


### P-P Cycles

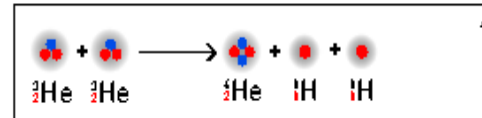
#### p-p reaction



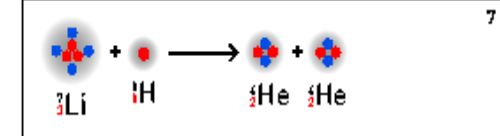
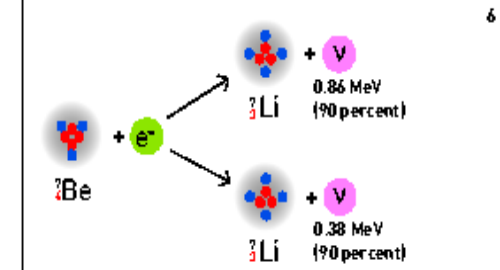
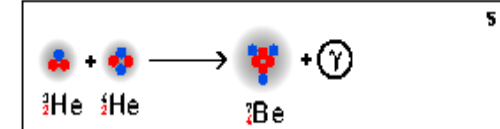
#### «pep» reaction (one time in 400)



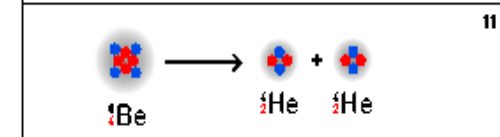
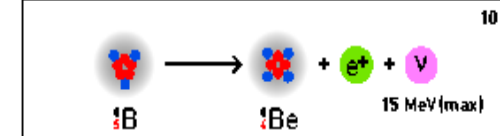
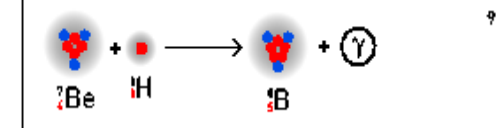
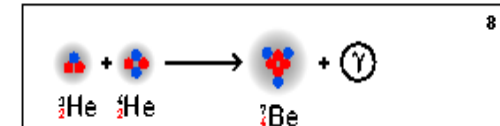
#### branch 1 (85%)



#### branch 2 (15%)



#### branch 3 (0.01%)



# How do Reactions Change Compositions?

- reaction between target  $j$  and projectile  $k$

$$\sigma = \frac{\# \text{ reactions per sec and target } j}{\text{flux of incoming projectiles } k} = \frac{r/n_j}{n_k v}$$

- for specific (velocity) distributions

$$r_{j,k} = \int \sigma |\vec{v}_j - \vec{v}_k| d^3 n_j d^3 n_k$$

- for Maxwell-Boltzmann distributions  $r_{j,k} = \langle \sigma v \rangle_{j,k} n_j n_k$

$$\langle \sigma v \rangle_{j,k} = \left( \frac{8}{\mu \pi} \right)^{1/2} (kT)^{-3/2} \int_0^\infty E \sigma(E) e^{-E/kT} dE$$

# Brief Summary of Burning Stages (Major Reactions)

## 1. Hydrogen Burning

$$T = (1-4) \times 10^7 \text{K}$$

pp-cycles  $\rightarrow$



CNO-cycle  $\rightarrow$  slowest reaction



## 2. Helium Burning

$$T = (1-2) \times 10^8 \text{K}$$



## 3. Carbon Burning

$$T = (6-8) \times 10^8 \text{K}$$



## 4. Neon Burning

$$T = (1.2-1.4) \times 10^9 \text{K}$$



## 5. Oxygen Burning

$$T = (1.5-2.2) \times 10^9 \text{K}$$



## 6. “Silicon” Burning

$$T = (3-4) \times 10^9 \text{K}$$

(all) photodisintegrations and capture reactions possible

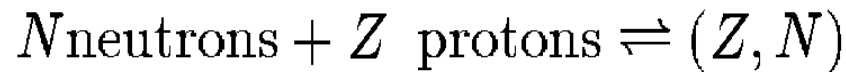
$\Rightarrow$  thermal (chemical) equilibrium

ongoing  
measurements  
of key fusion  
reactions at low  
energies

$$30kT = 4\text{MeV}$$

# Global Chemical (=Nuclear Statistical) Equilibrium (NSE)

$$\begin{aligned}\bar{\mu}(Z, N) + \bar{\mu}_n &= \bar{\mu}(Z, N + 1) \\ \bar{\mu}(Z, N) + \bar{\mu}_p &= \bar{\mu}(Z + 1, N)\end{aligned}\quad \bar{\mu}_i = kT \ln \left( \frac{\rho N_A Y_i}{G_i} \left( \frac{2\pi\hbar^2}{m_i kT} \right)^{3/2} \right) + m_i c^2$$



$$N \bar{\mu}_n + Z \bar{\mu}_p = \bar{\mu}_{Z,N}.$$

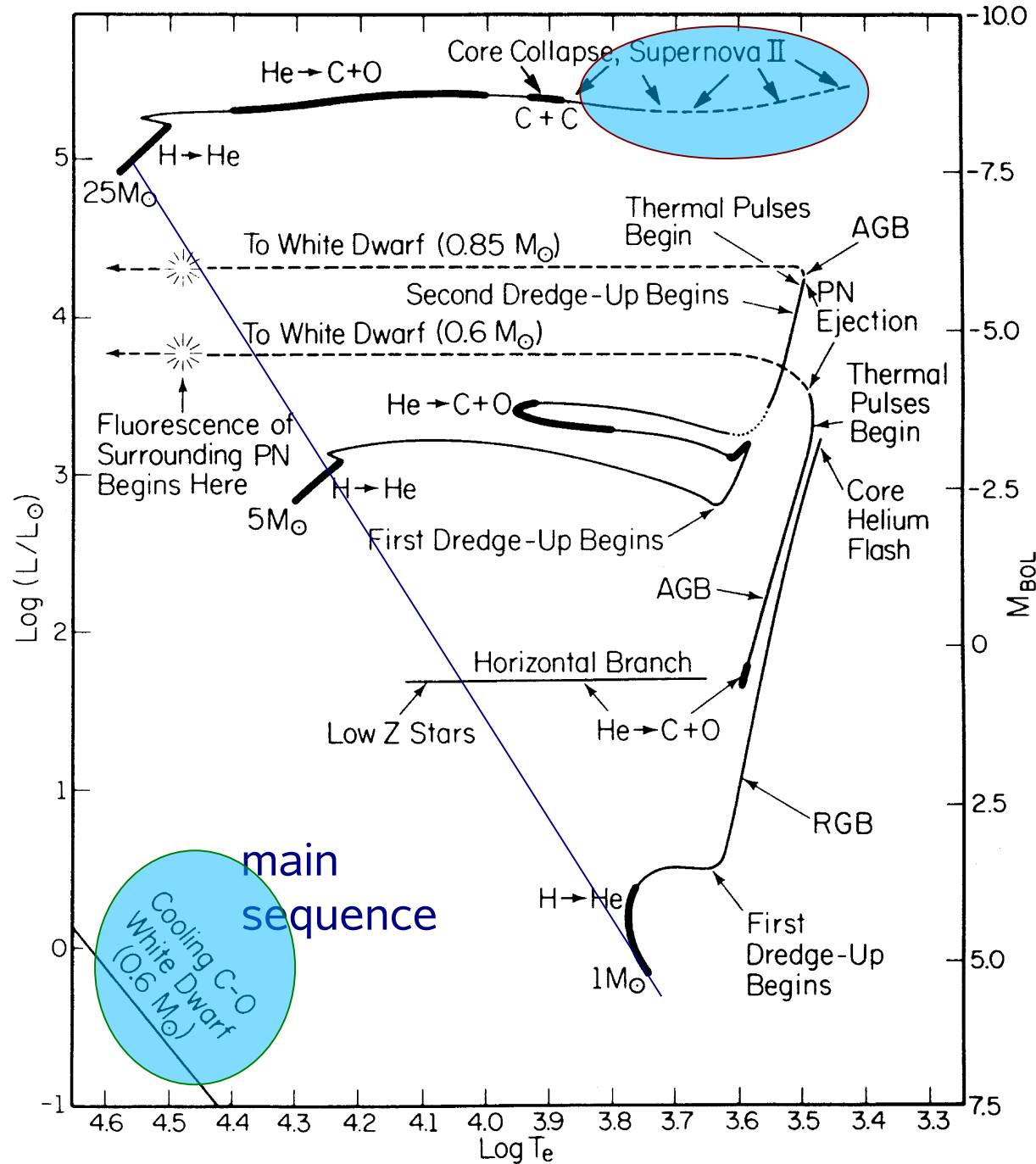
$$Y(Z, N) = G_{Z,N} (\rho N_A)^{A-1} \frac{A^{3/2}}{2^A} \left( \frac{2\pi\hbar^2}{m_u kT} \right)^{\frac{3}{2}(A-1)} \exp(B_{Z,N}/kT) Y_n^N Y_p^Z$$

$$\sum_i A_i Y_i = 1$$

$$\sum_i Z_i Y_i = Y_e$$



# Astrophysical Sites



Hertzsprung-Russell Diagram of Stellar Evolution from Iben, showing as end stages

- white dwarfs

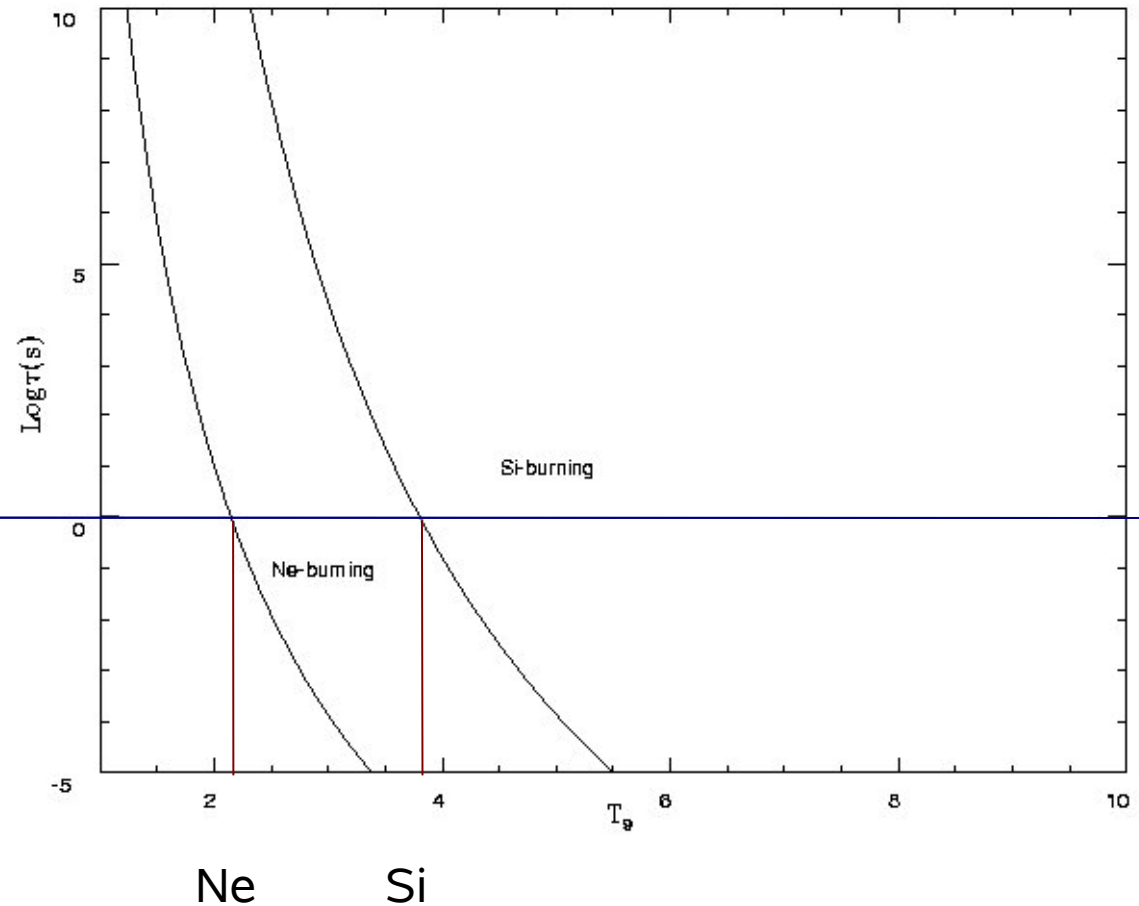
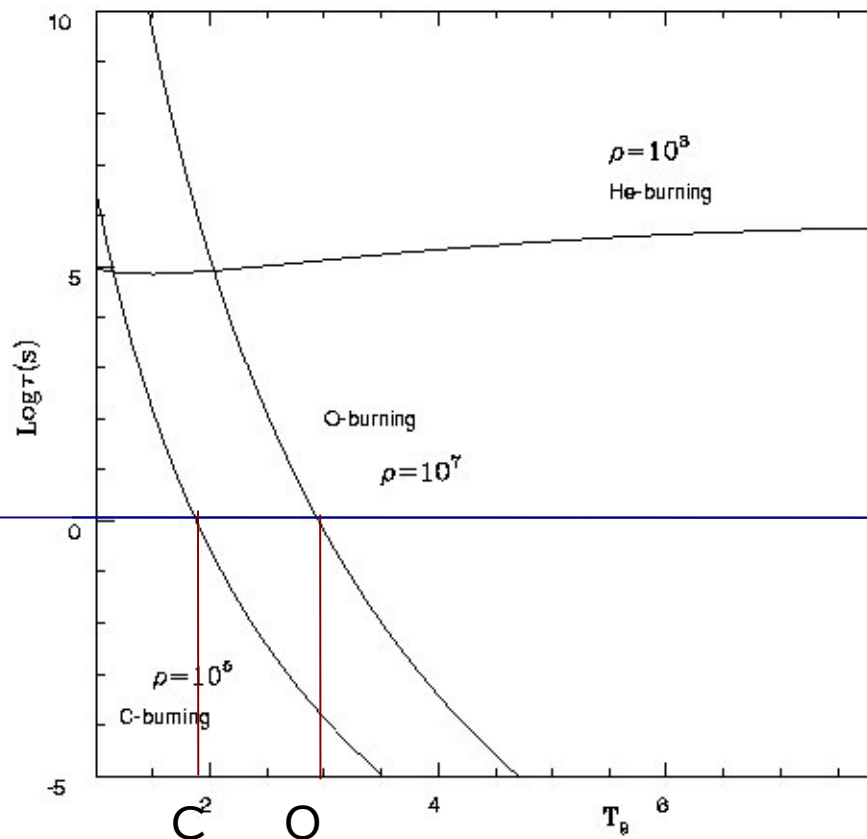
and

- core collapse (supernovae/neutron stars, black holes, GRBs?)

*influence of reaction cross sections, e-capture in late burning stages, metallicity, rotation, magnetic fields, stellar winds on final outcome*



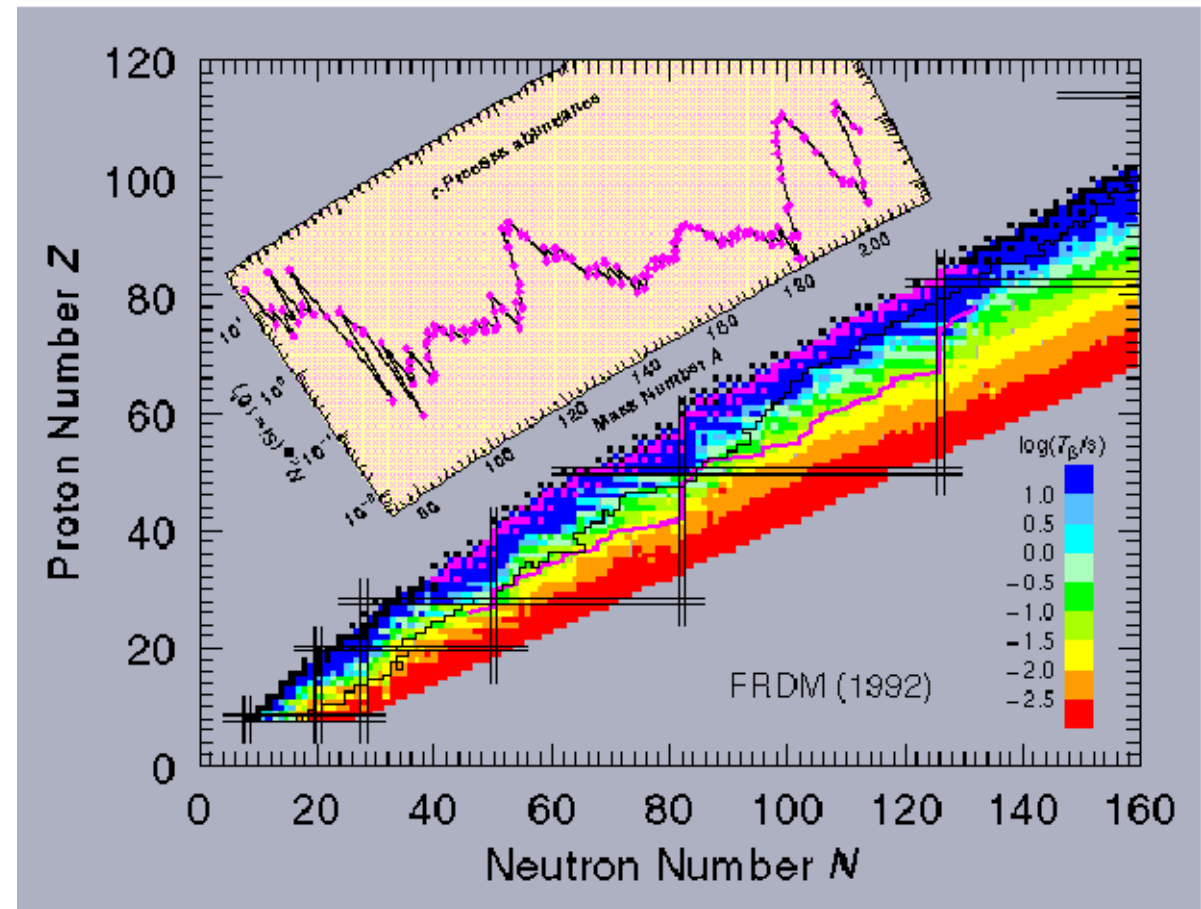
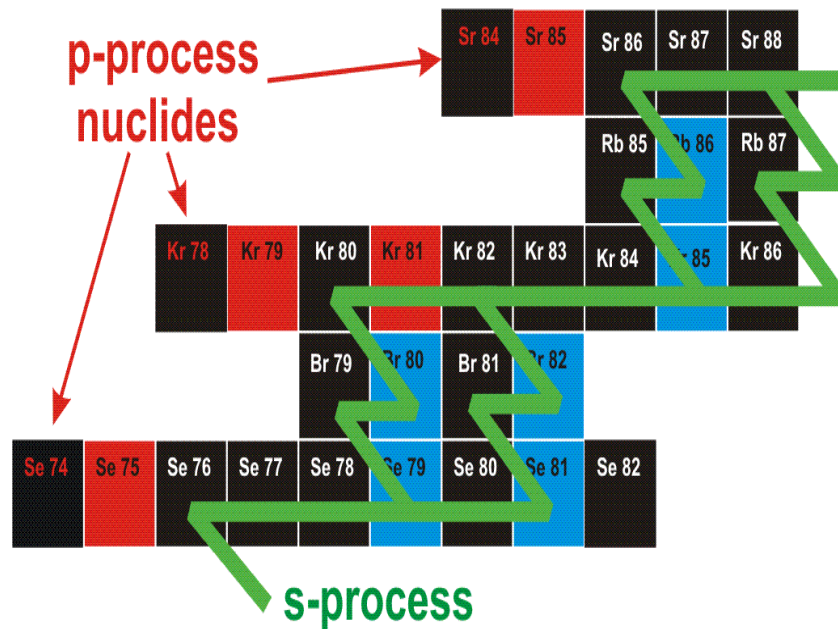
# Explosive Burning



typical explosive burning process timescale order of seconds:  
 fusion reactions (He, C, O) density dependent (He quadratic,  
 C,O linear)

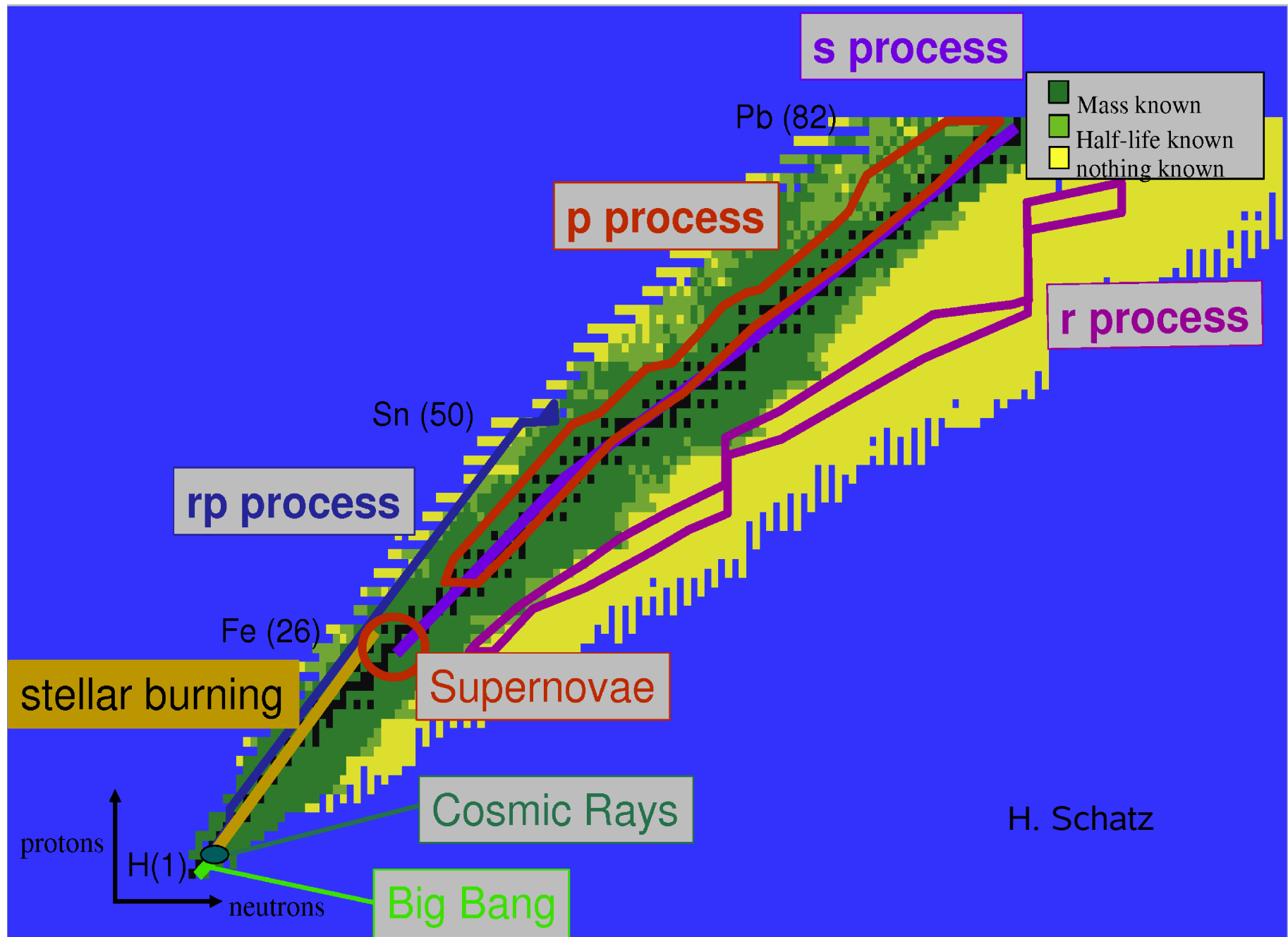
photodisintegrations (Ne, Si) not density dependent

# s-, r- and p-Process



P. Möller

# All Processes in the Nuclear Chart



# Mass predictions (far from stability):

Is there an accuracy limit?

## Comparison to NUBASE (2001) // (2003)

FRDM (1992)  $\sigma_{\text{rms}} = 0.669$  // **0.616** [MeV]

ETFSI-Q (1996)  $\sigma_{\text{rms}} = 0.818$  // **0.729** [MeV]

existing approaches:  
Finite Range Droplet  
Model,  
Extended Thomas Fermi,  
Hartree-Fock Bogoliubov

with new deformation shapes/symmetries FRDM expects to  
improve by about 0.1

HFB-2 (2002)  $\sigma_{\text{rms}} = 0.674$  [MeV]

HFB-3 (2003)  $\sigma_{\text{rms}} = 0.656$  [MeV]

HFB-4 (2003)  $\sigma_{\text{rms}} = 0.680$  [MeV]

HFB-8 (2004)  $\sigma_{\text{rms}} = 0.635$  [MeV]

HFB-9 (2005)  $\sigma_{\text{rms}} = \mathbf{0.733}$  [MeV]

HFB-14 (2007)  $\sigma_{\text{rms}} = 0.729$  [MeV]

## Other microscopic approaches

- united energy density functional (UENDEF)

- relativistic mean field

Test with Rare Isotope Beam  
Facilities

- RIKEN, GSI/FAIR, RIA2?

- and related theory efforts (e.g. ENSAR)

# “Historical” Burning Processes (B<sup>2</sup>FH)

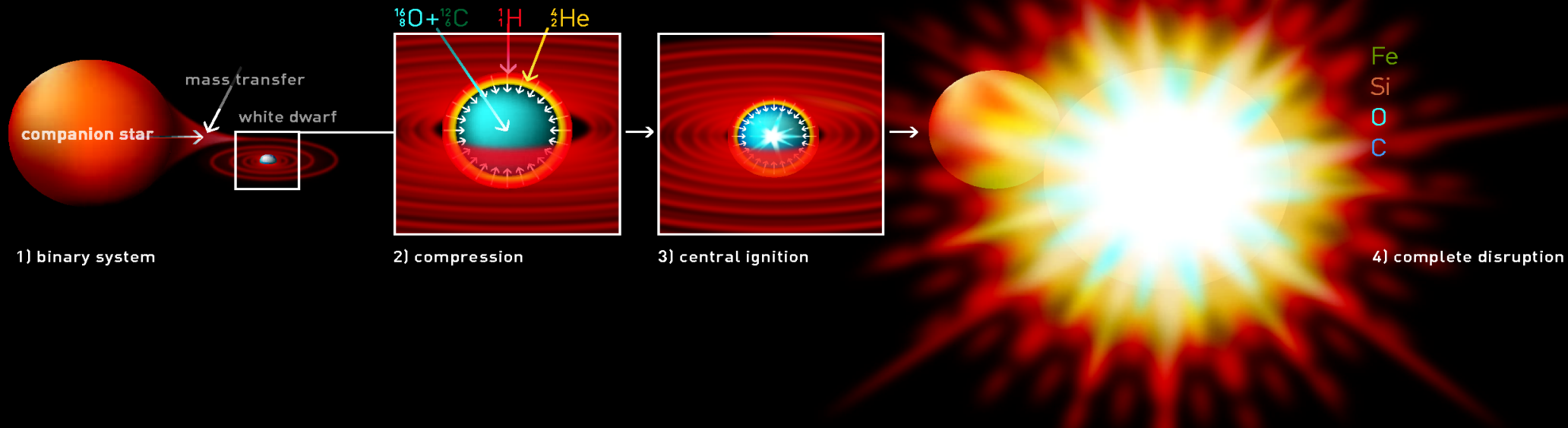
- H-Burning
- He-Burning
- alpha-  
Process
- e-Process
- s-Process
- r-Process
- p-Process
- x-Process

## Present Understanding

- H-Burning
- He-Burning
- expl. C, Ne, O-Burning, incomplete Si-Burning
- explosive Si-Burning
  - about 70% normal freeze-out,  $Y_e=0.42-47$ , about 30% alpha-rich freeze-out,  $Y_e=0.5$
- s-Process (core and shell He-burning, neutrons from alpha-induced reactions on <sup>22</sup>Ne and <sup>13</sup>C)
- r-Process (see below)
- p-Process (see below)
- x-Process (light elements D, Li, Be, B [big bang, cosmic ray spallation and neutrino nucleosynthesis])
- rp-Process and vp-Process not yet known

# Type Ia Supernovae from Accretion in Binary Stellar Systems

## Type I (a) Supernova



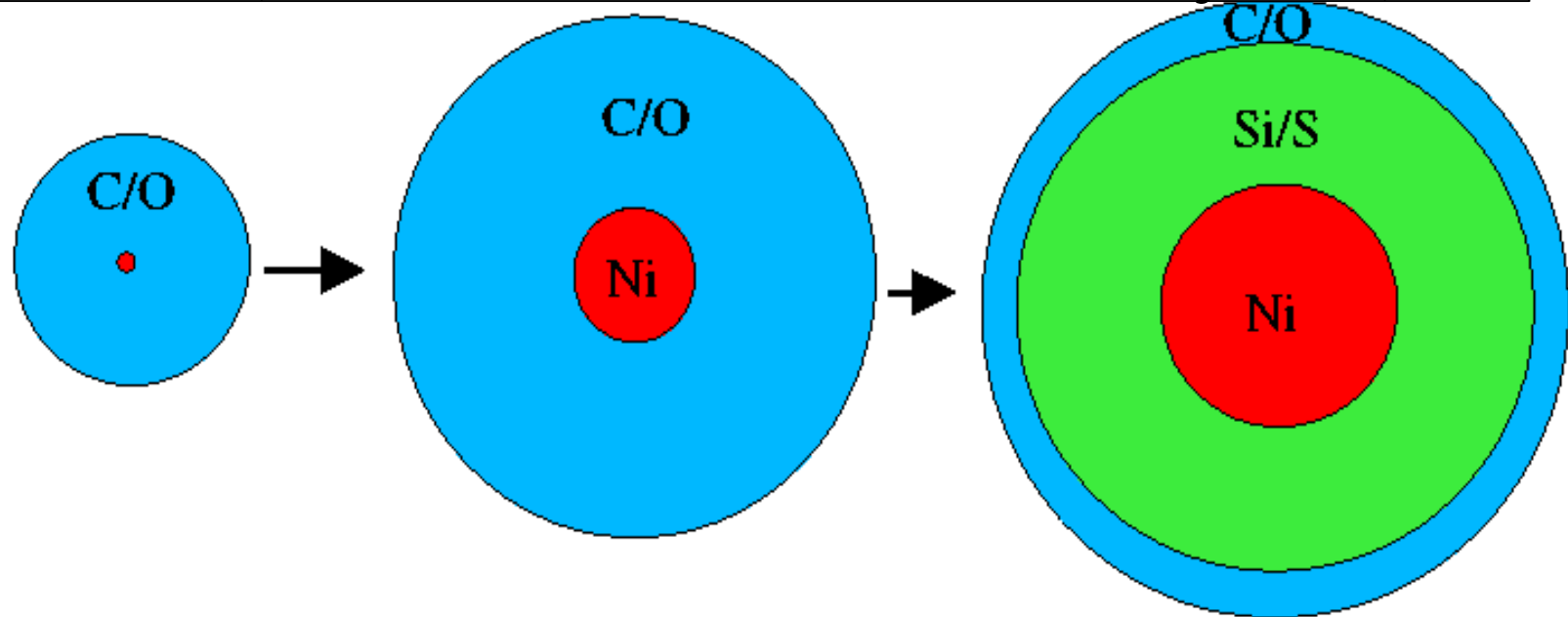
binary systems with accretion onto one compact object can lead (depending on accretion rate) to explosive events with thermonuclear runaway (under electron-degenerate conditions)

- white dwarfs (novae, type Ia supernovae)
- neutron stars (type I X-ray bursts, superbursts?)



# Back of the Envelope SN Ia

e.g. W7 (Nomoto, Thielemann, Yokoi 1984); delayed detonations (Khokhlov, Höflich, Müller; Woosley et al.)



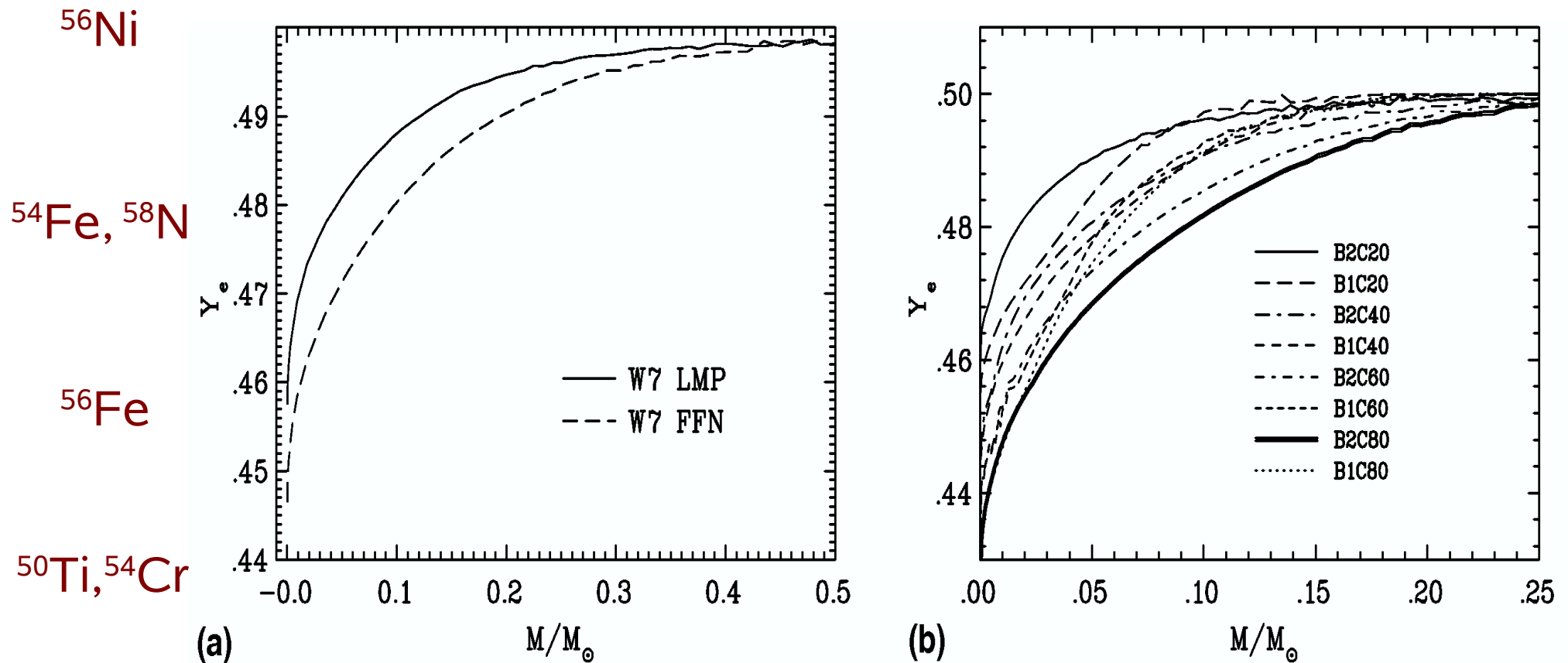
$M_{ch} \approx 1.4 M_{\odot}$  of  $^{12}\text{C}/^{16}\text{O}=1$  WD  $\rightarrow 1.398776 M_{\odot} \text{ } ^{56}\text{Ni}$

$\rightarrow 2.19 \times 10^{51}$  erg -  $E_{grav} \approx (5 - 6) \times 10^{50}$  erg

reduction due to intermediate elements like Mg, Si, S, Ca

$\rightarrow 1.3 \times 10^{51}$  erg in spherically symmetric models description of the burning front propagation (with hydrodynamic instabilities) determines outcome!

# Neutronization via electron capture (high Fermi energies at central densities)

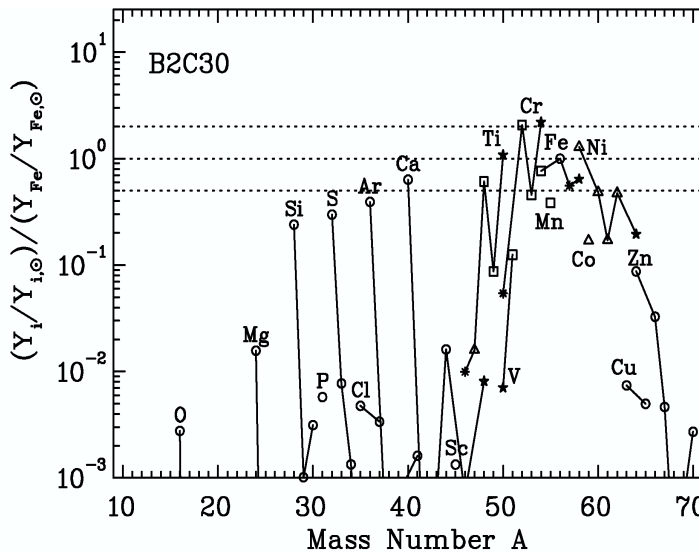
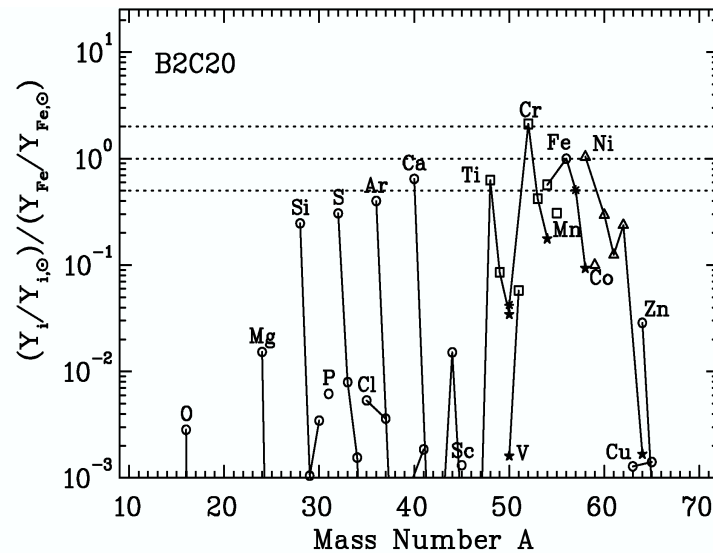


(a) Test for influence of new shell model electron capture rates  
(including pf- shell Langanke, Martinez-Pinedo 2003)

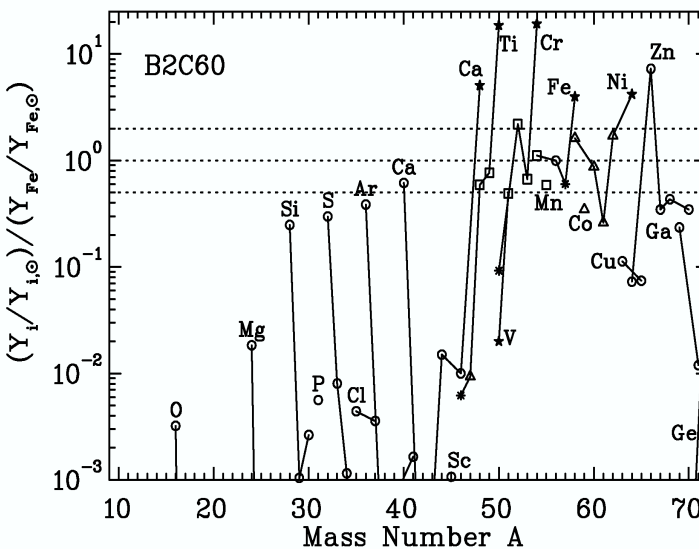
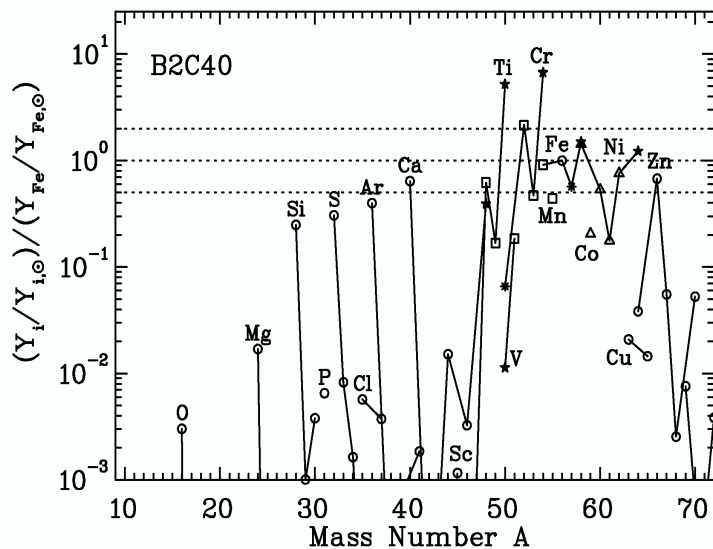
(b) Test for burning front propagation speed (Brachwitz et al. 2001)  
*direct influence on dominant Fe-group composition resulting from SNe Ia*

# Ignition density determines Ye and neutron-richness of (60-70% of) Fe-group

FKT et al. (2004)



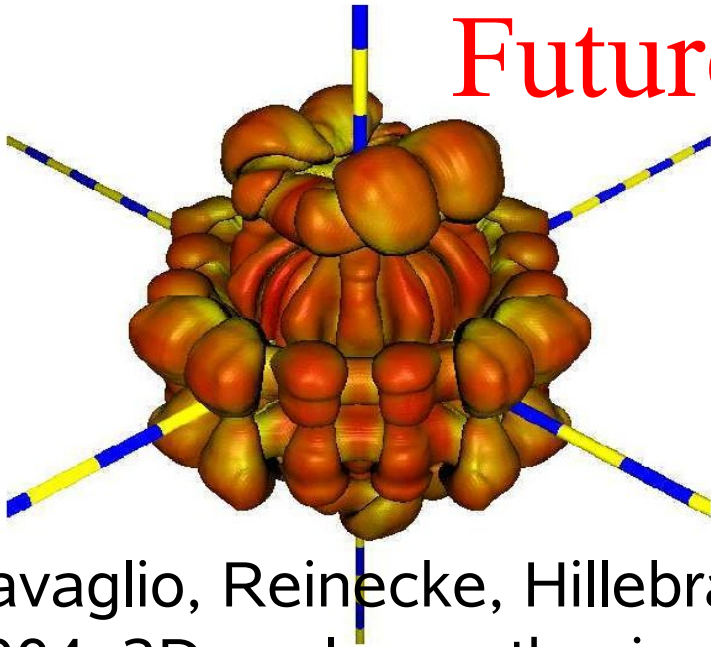
results of explosive C, Ne, O and Si-burning:  
Fe-group to alpha-elements 2/1-3/1



SNe Ia dominate Fe-group, overabundances by more than factor 2 not permitted

→ maximum central density  $3 \times 10^9 \text{ g cm}^{-3}$

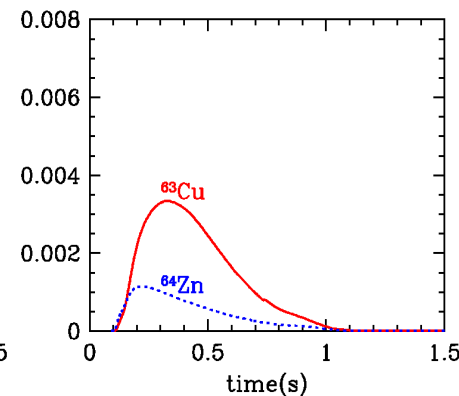
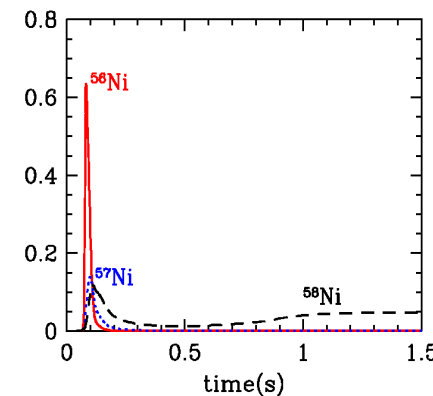
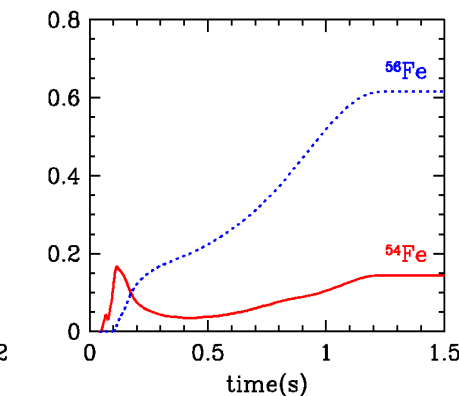
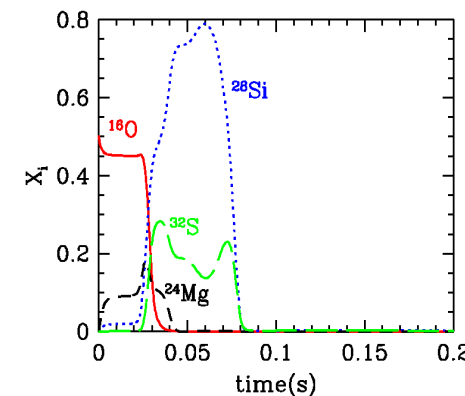
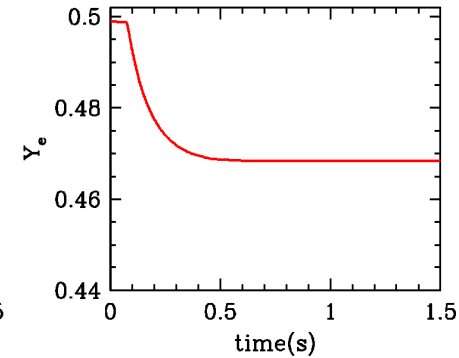
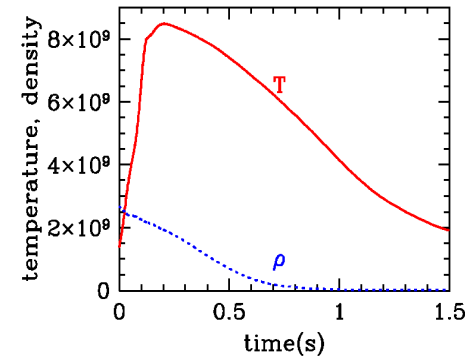
# Future 3D Models



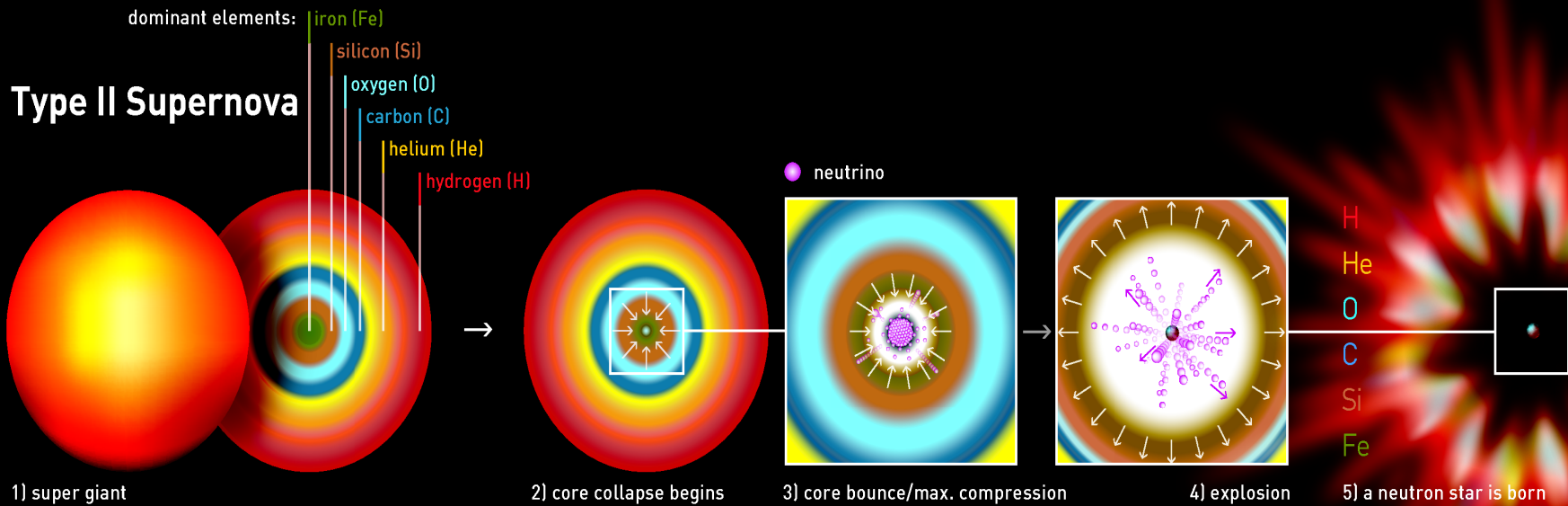
Travaglio, Reinecke, Hillebrandt, FKT (2004, 3D nucleosynthesis with tracer particles)

consistent treatment needed instead of parametrized spherical propagation, MPA Garching (Röpke et al. 2007), U. Chicago/SUNY Stony Brook (Calder et al. 2007)

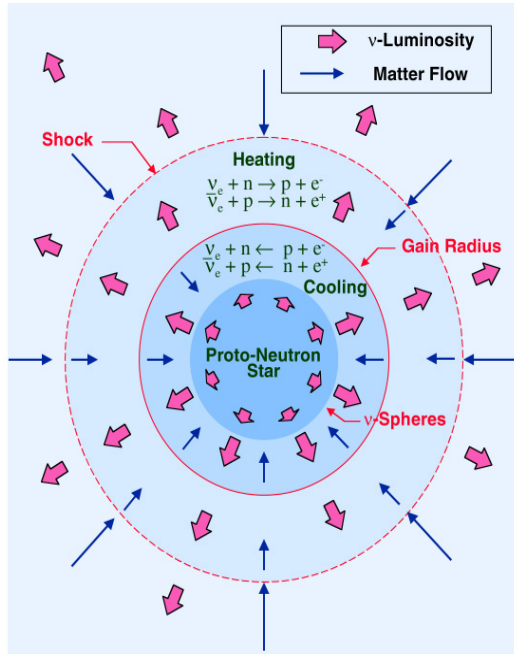
- *distribution of ignition points uncertain*
- *hydrodynamic instabilities determine propagation of burning*
- *deflagration/detonation transition*



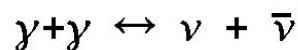
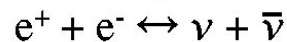
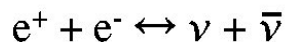
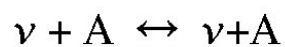
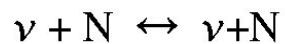
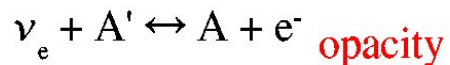
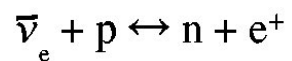
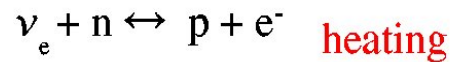
# Core Collapse Supernovae from Massive Stars



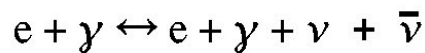
# Neutrino-driven Core Collapse Supernovae



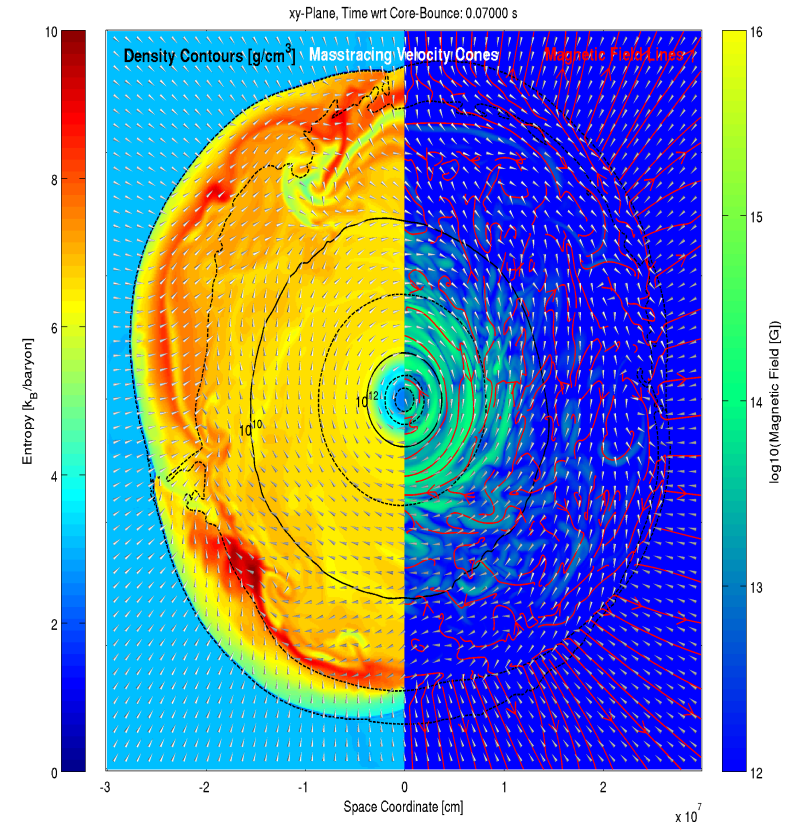
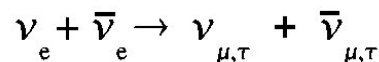
## Simulations with Rotation and Magnetic Fields



also



and

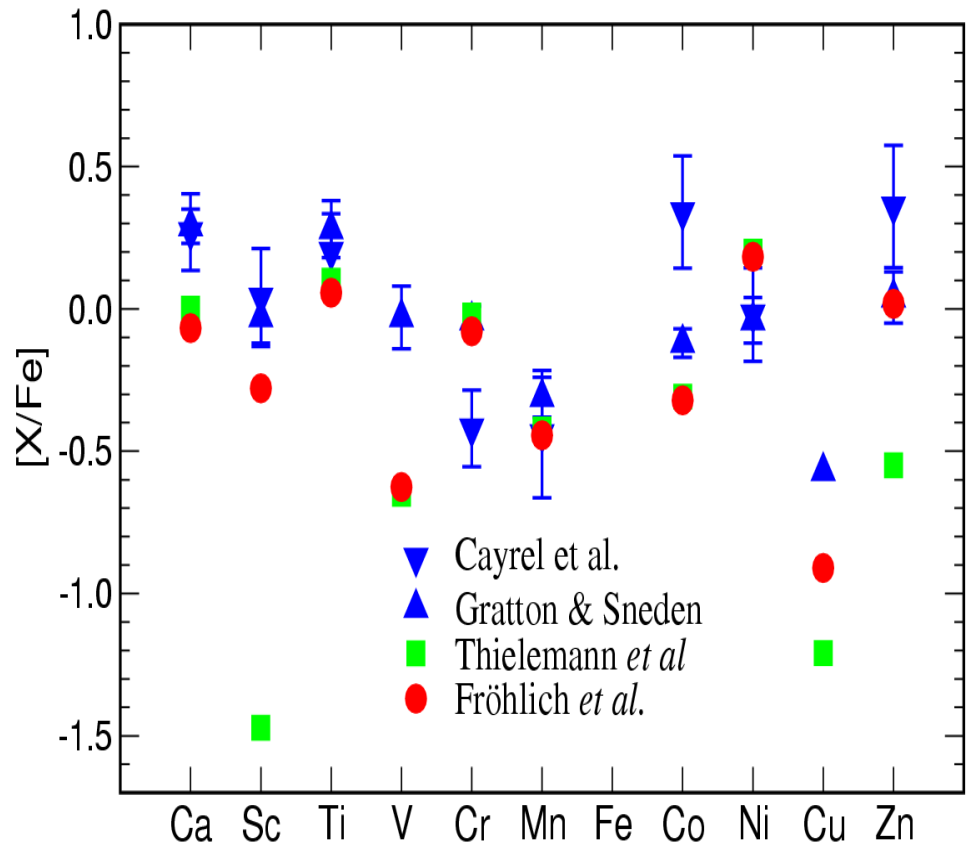
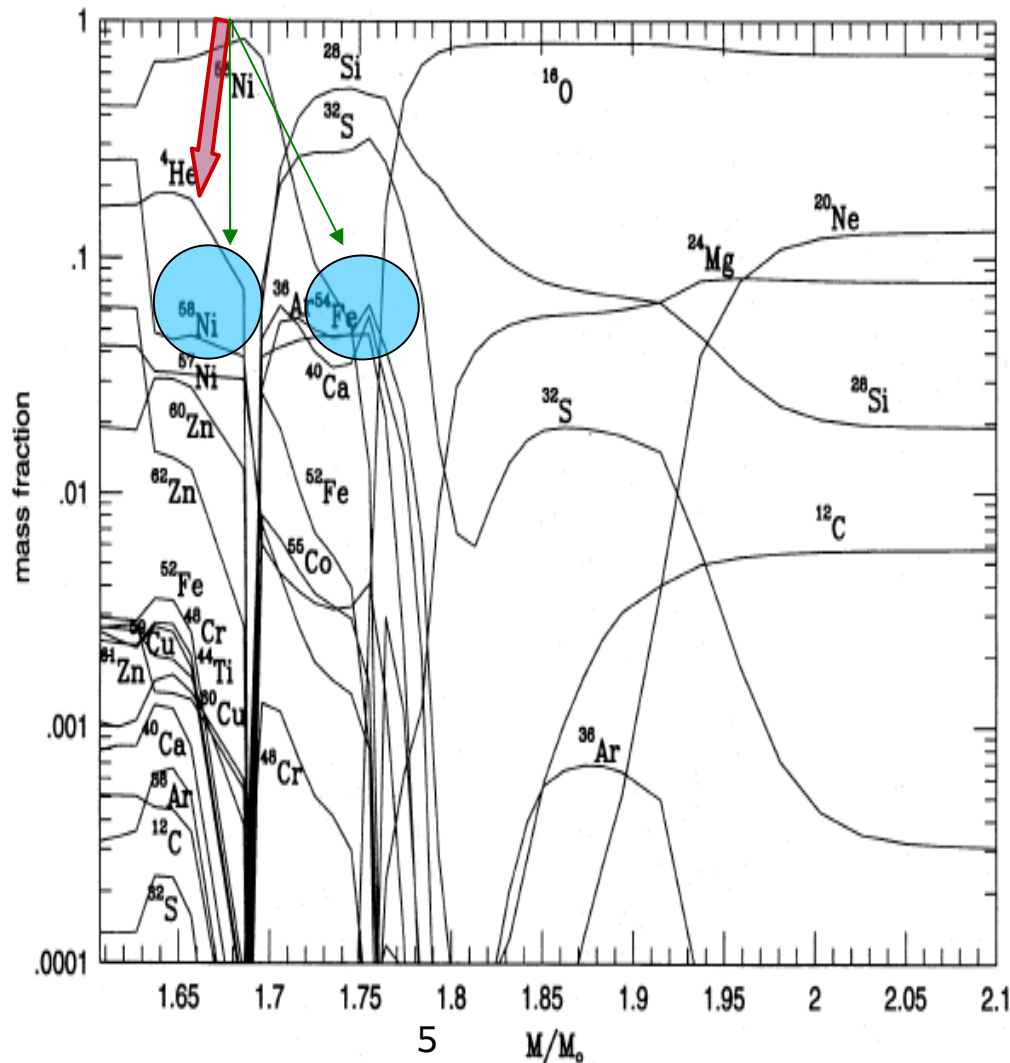


entropy and magnetic field strength 0.07s after bounce

grav. wave signal should be seen with LIGO at 10kpc



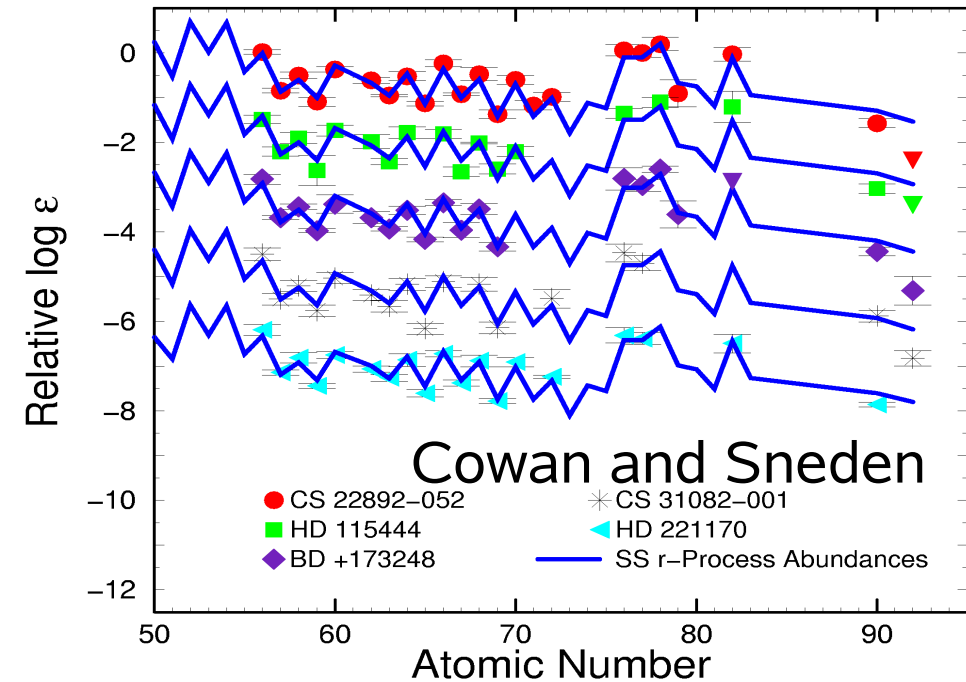
Nucleosynthesis problems in “induced” piston or thermal bomb models  
utilized up to present to obtain explosive nucleosynthesis yields with induced  
explosion energies of  $10^{51}$  erg



Fröhlich et al. (2004, 2006a), see also  
Pruet et al. (2005), improved Fe-group  
composition

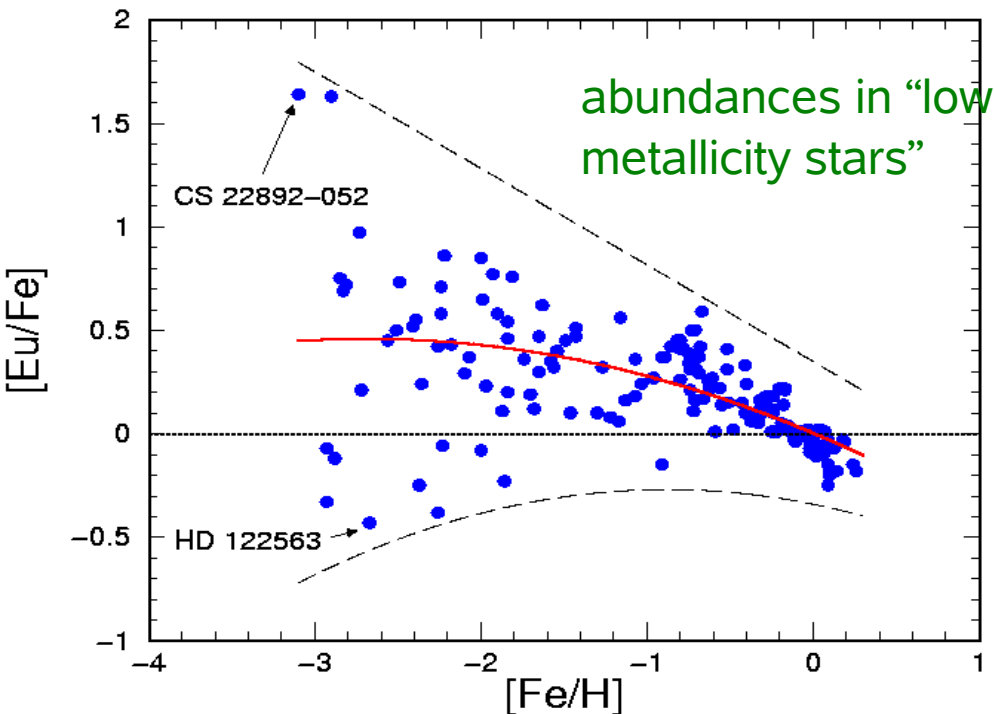
prior results of Thielemann, Nomoto, Woosley, Chieffi .. made use of initial stellar structure (and  $Y_e$ !)  
when inducing artificial explosion. This neglects the effect of the explosion mechanism on the  
innermost zones, causes strange overproductions of Ni isotopes and does not go much beyond Ni!

# Observational Constraints on r-Process Sites

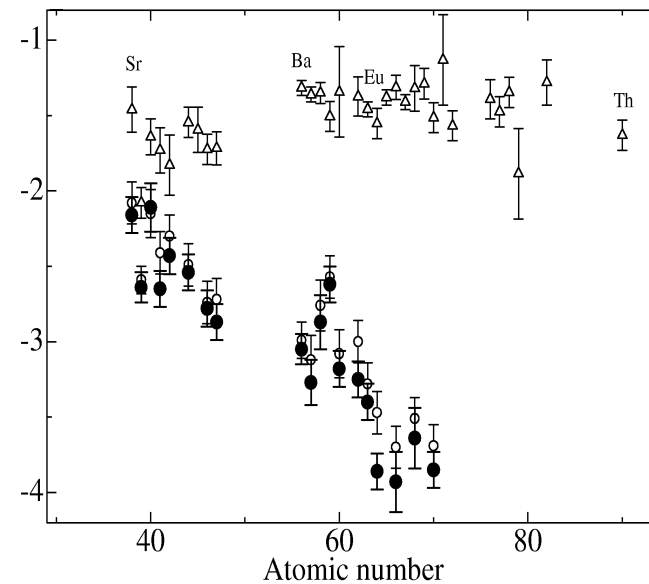


apparently uniform abundances above  $Z=56$  (and up to  $Z=82$ ?) -> “unique” astrophysical event which nevertheless consists of a superposition of ejected mass zones

“rare” event, which must be related to massive stars due to “early” appearance at low metallicities (behaves similar to SN II products like O, but with much larger scatter)



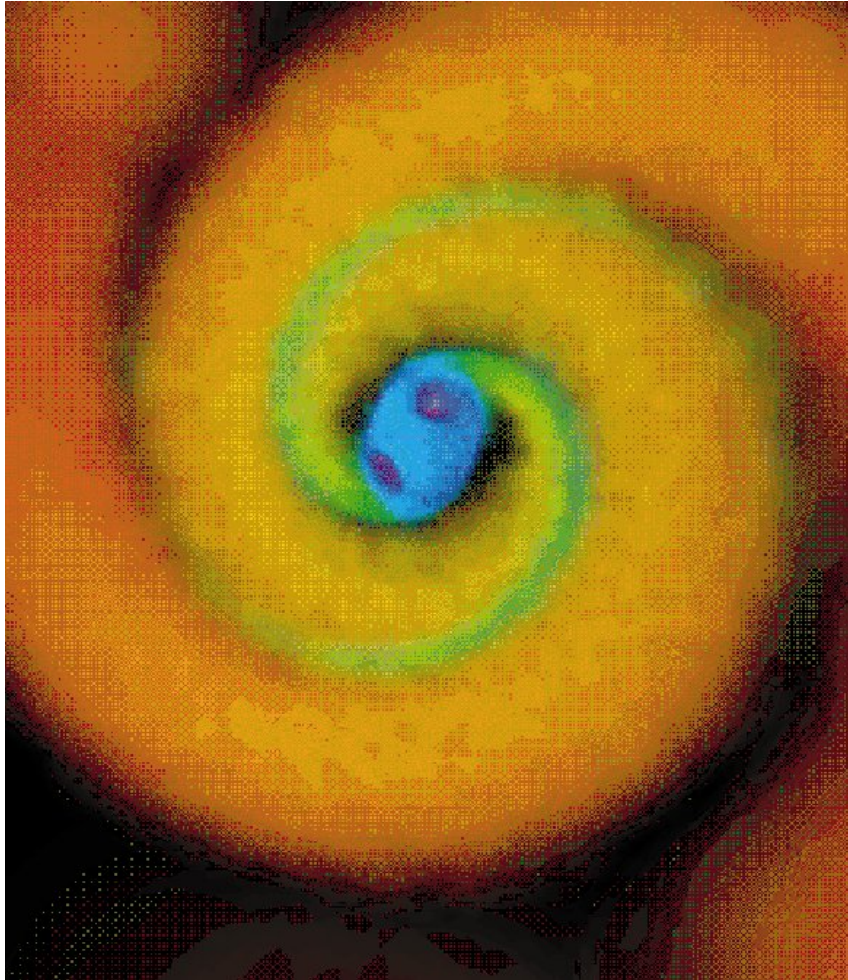
## Observations of the weak r-process?



Honda et al. (2007)

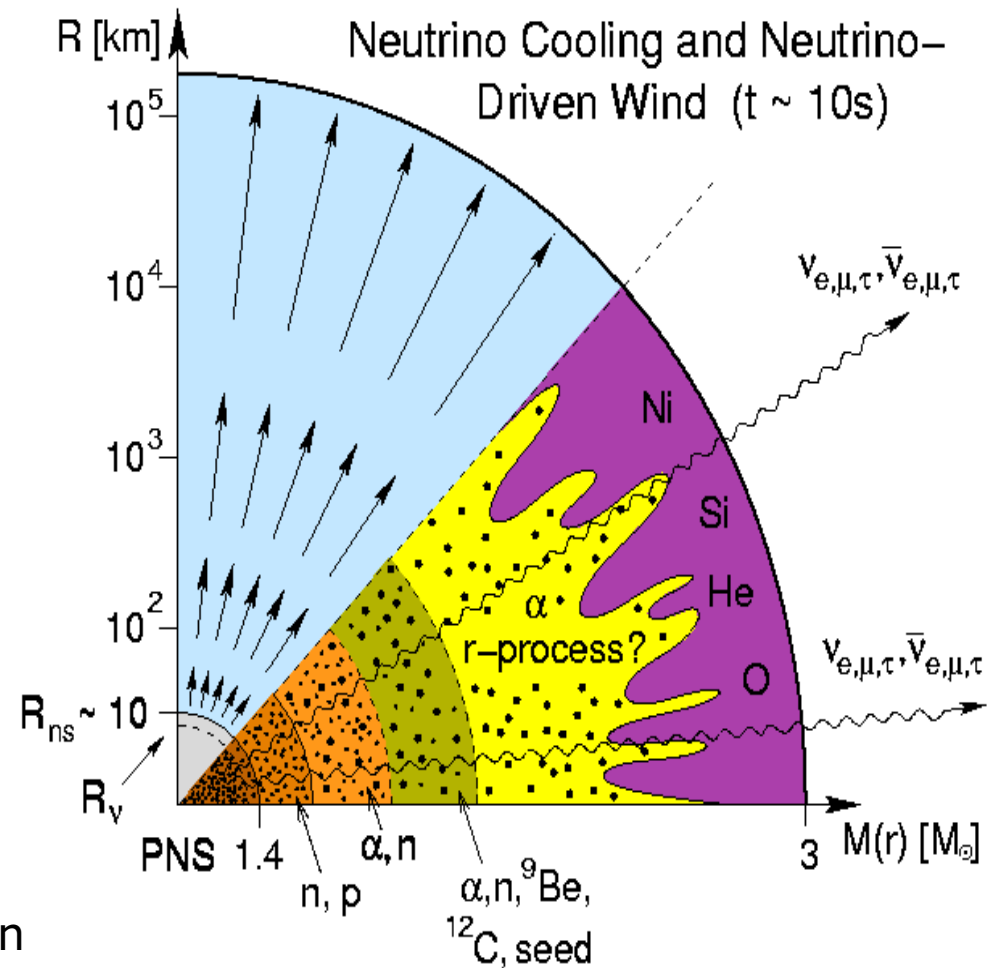
# What is the site of the r-process?

from S. Rosswog



NS mergers, BH-NS mergers, problems: ejection too late in galactic evolution (or alternatively polar jets from supernovae, Cameron 2003)

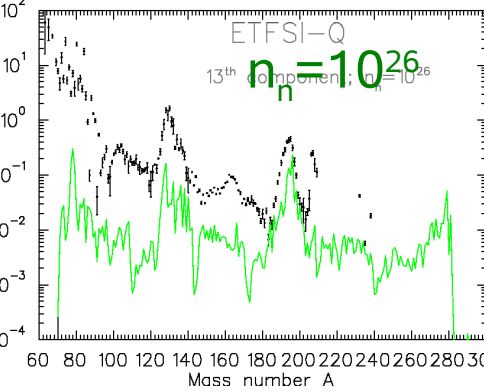
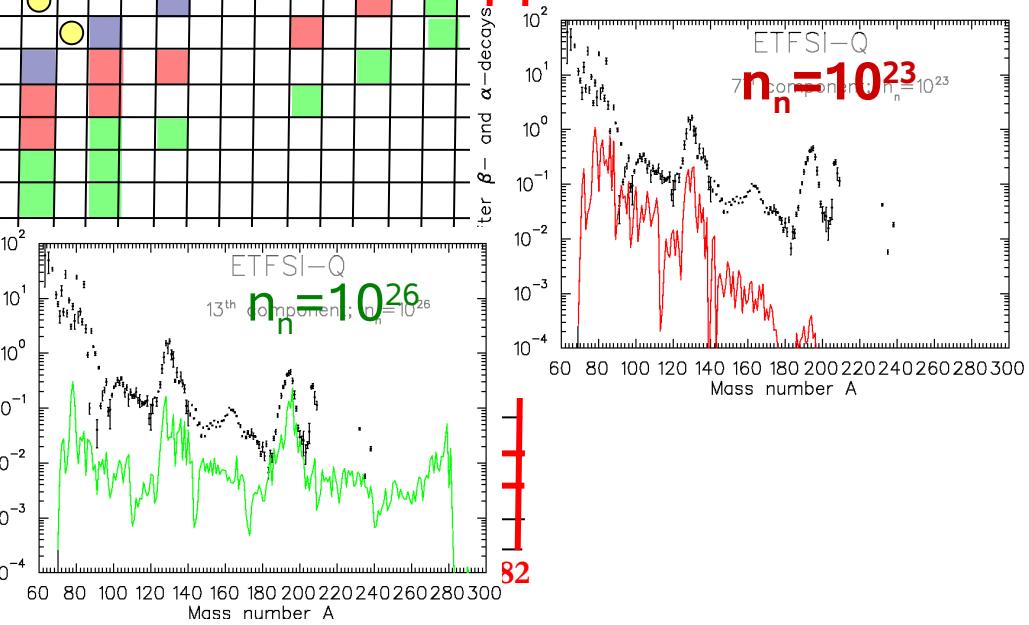
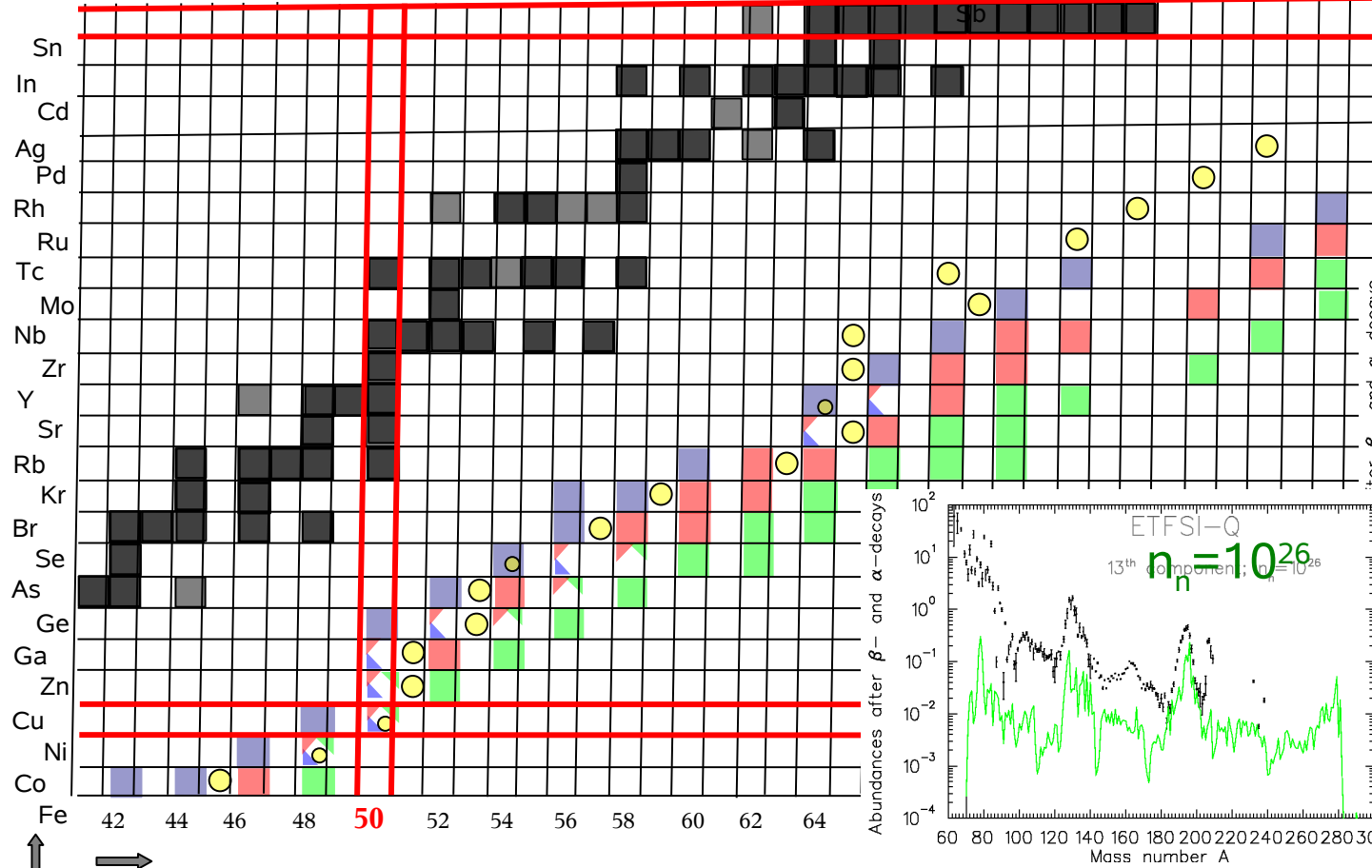
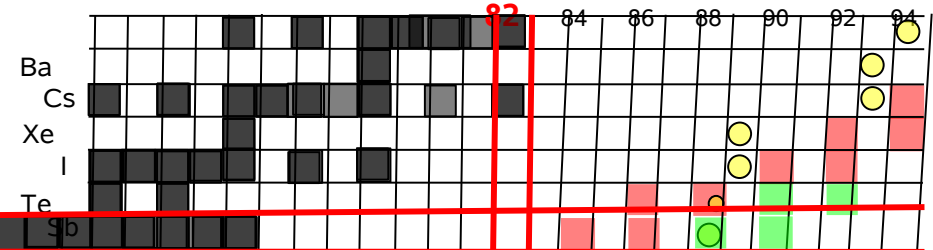
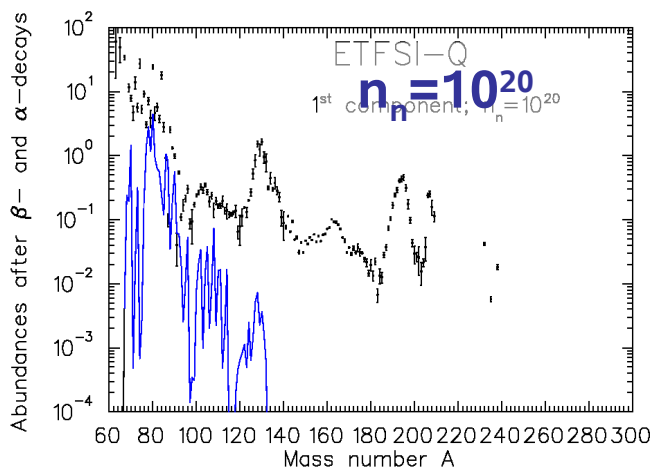
from H.-T. Janka



SN neutrino wind, problems: high enough entropies attained? neutrino properties???

# (classical) r-Process paths for $n_n=10^{20}$ , $10^{23}$ and $10^{26}$ and $T_9=1.35$

K.-L. Kratz

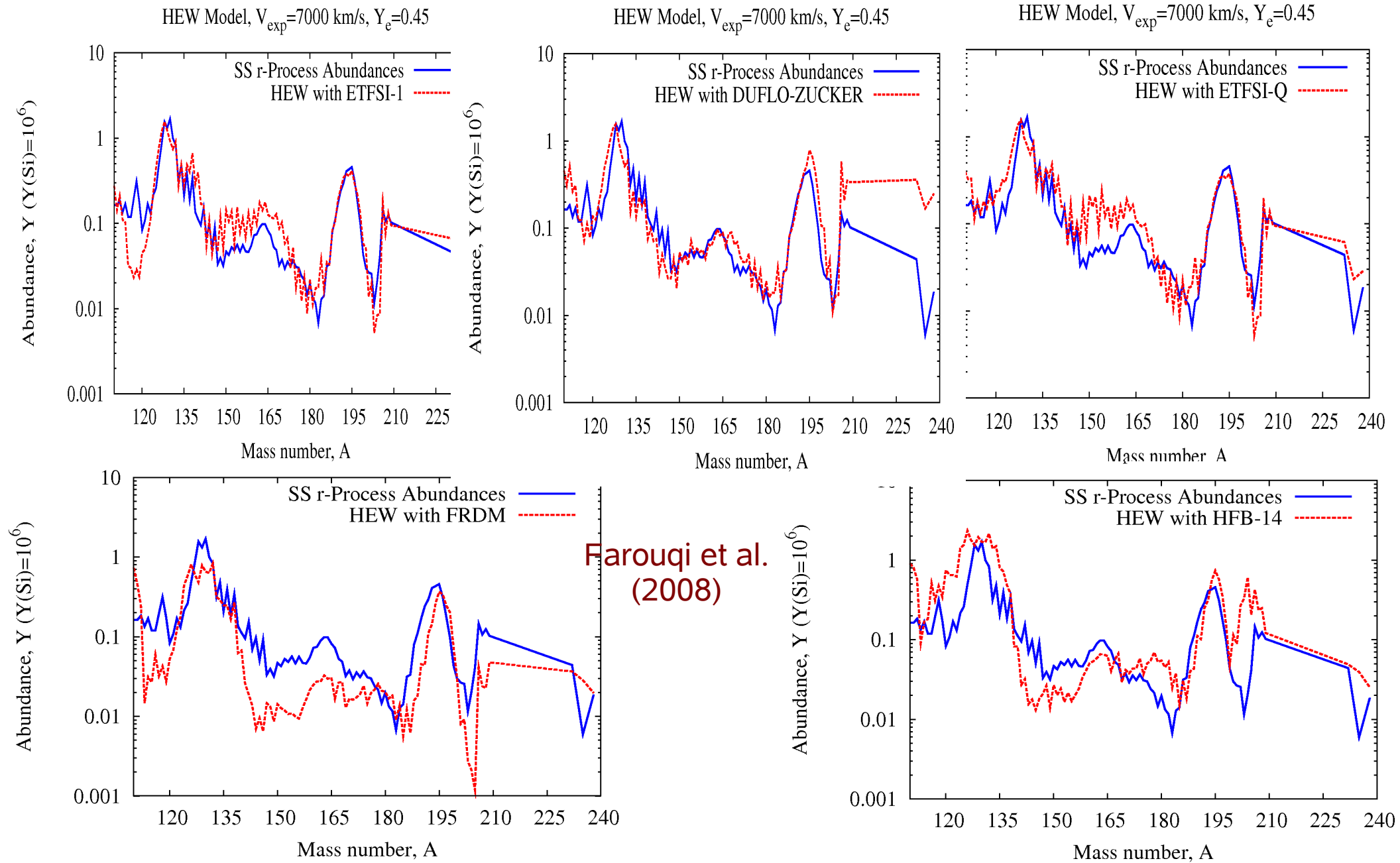


$\uparrow$   
**Z**

$\rightarrow$   
**N**

„waiting-point“ isotopes for  $n_n=10^{20}$ ,  $10^{23}$  and  $10^{26}$

# Superposition of entropies for different mass models

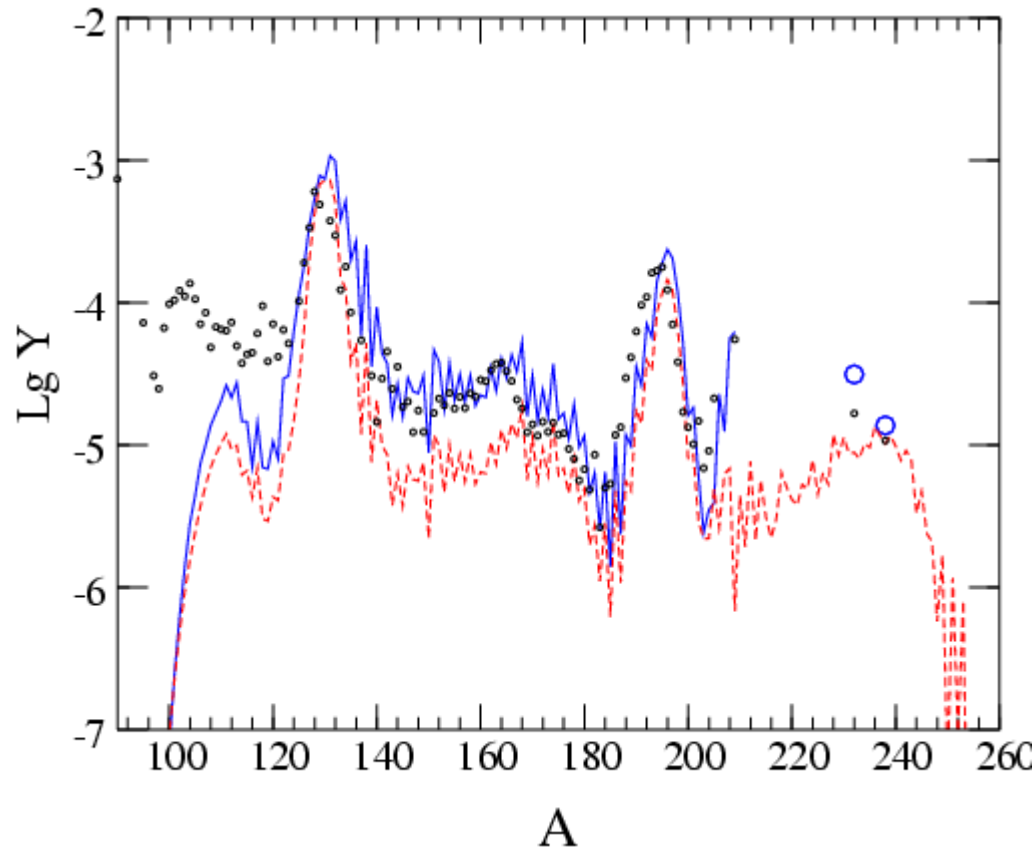


*we can test nuclear models with assumed conditions from stellar explosions, but the site is still open*

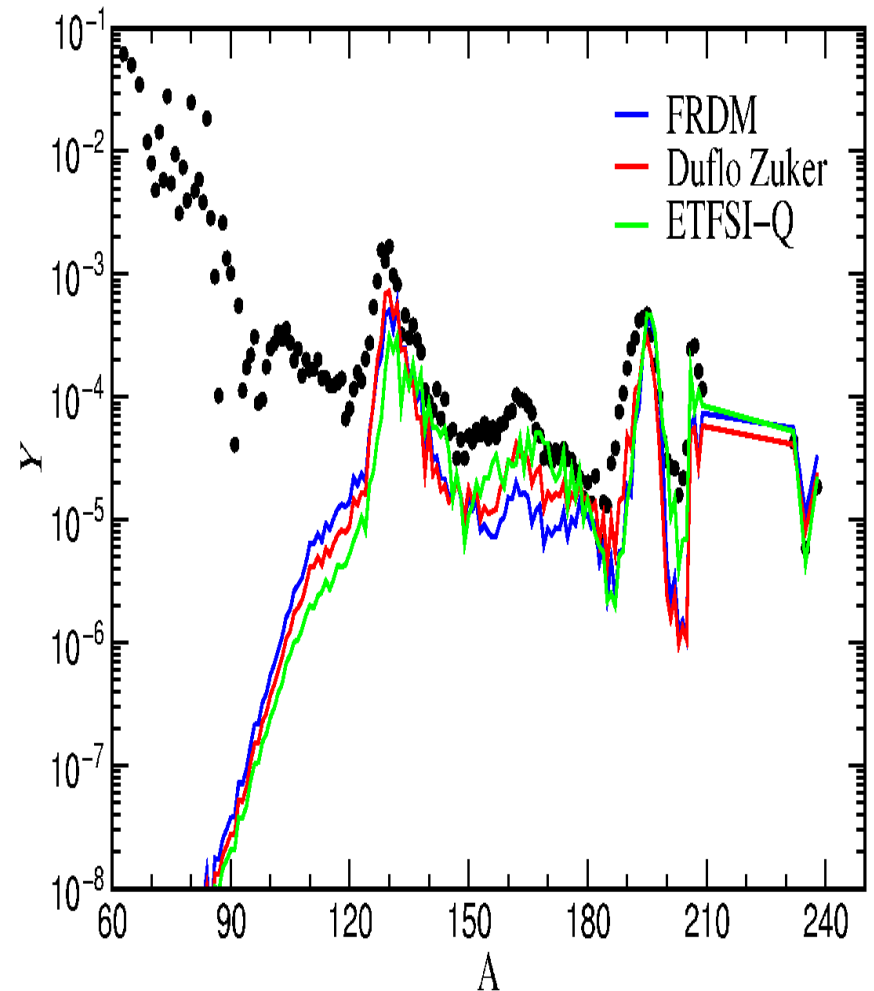


# Fission Cycling in Neutron Star Mergers

Trajectory from Freiburghaus, Rosswog, and Thielemann 1999  
( $Y_e = 0.1, n/Seed = 238$ ).



Panov and FKT (2007) with parametrized fission yield contribution



Martinez-Pinedo et al. (2007)

in principle contradicted from gal. evol. calc., but similar conditions in SN polar jets? (Cameron 2003)